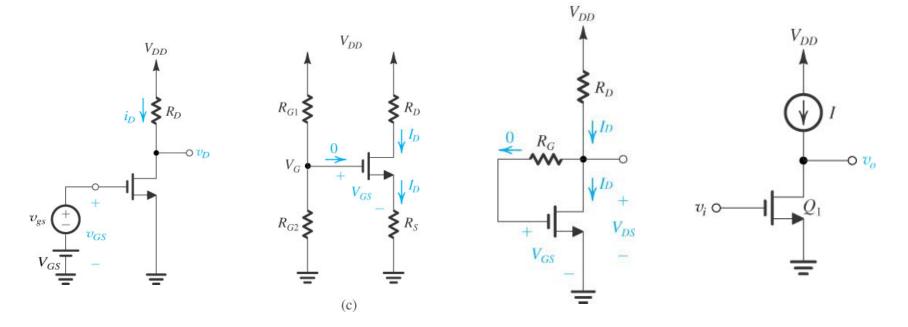
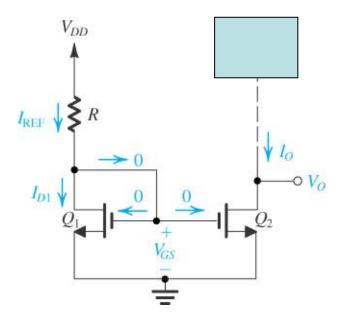
### Various bias techniques for MOSFET circuits



How do we make a constant current source with MOSFETs?

#### Constant current source:



(R can be outside the IC chip)

→ Current mirror

$$I_{D1} = \frac{1}{2} k_n \left( \frac{W}{L} \right)_1 \left( V_{GS} - V_{tn} \right)^2$$

$$\boldsymbol{I}_{D1} = \boldsymbol{I}_{REF} = \frac{\boldsymbol{V}_{DD} - \boldsymbol{V}_{GS}}{\boldsymbol{R}}$$

Assuming Q<sub>1</sub>, Q<sub>2</sub> have same properties,

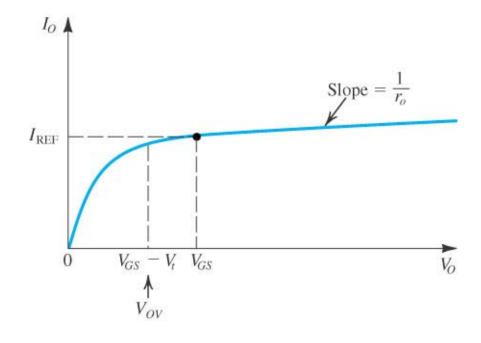
$$I_{O} = I_{D2} = \frac{1}{2} k_{n} \left( \frac{W}{L} \right)_{2} \left( V_{GS} - V_{tn} \right)^{2}$$

$$\frac{I_{O}}{I} = \frac{\left( W/L \right)_{2}}{\left( W/L \right)}$$

Limitation on 
$$V_o$$
?  $V_o \ge V_{GS} - V_{tn}$ 



### Mismatches between I<sub>REF</sub> and I<sub>O</sub>



### Channel-length modulation

For two identical  $Q_1$  and  $Q_2$  $I_O = I_{REF}$  when  $V_0 = V_{GS}$ 

As  $V_O$  increased,  $I_O$  increases from  $I_{REF}$ 

$$\boldsymbol{I}_{O} = \boldsymbol{I}_{REF} + \frac{\boldsymbol{V}_{O} - \boldsymbol{V}_{GS}}{\boldsymbol{r}_{0}}$$

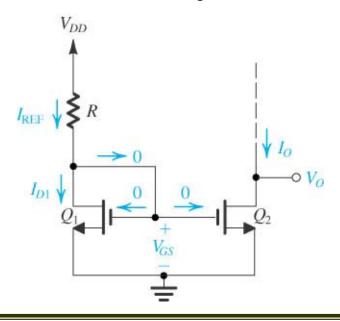
Since 
$$r_0 \simeq \frac{V_A}{I_{REF}}$$

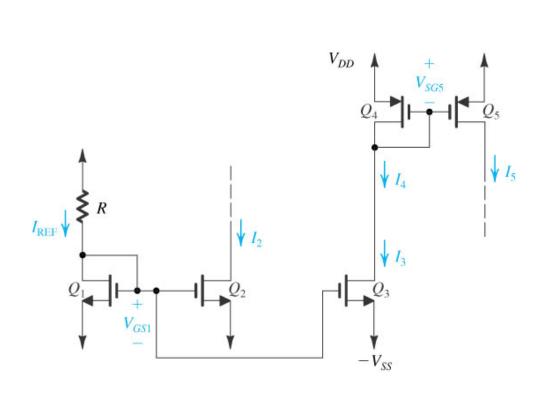
$$\boldsymbol{I}_{O} = \boldsymbol{I}_{REF} + \frac{\boldsymbol{V}_{O} - \boldsymbol{V}_{GS}}{\boldsymbol{V}_{A}} \cdot \boldsymbol{I}_{REF} = \boldsymbol{I}_{REF} \left( 1 + \frac{\boldsymbol{V}_{O} - \boldsymbol{V}_{GS}}{\boldsymbol{V}_{A}} \right)$$

### Example 6.5

 $V_{DD}$ =3V,  $Q_1$  and  $Q_2$  are identical with L= 1 $\mu$ m, W=100 $\mu$ m, V<sub>t</sub>=0.7V, k<sub>n</sub>'=200 $\mu$ A/V<sup>2</sup>, V<sub>A</sub>' (Early voltage per L) =20V/ $\mu$ m

- 1. Determine R for  $I_0$ =100 $\mu$ A.
- 2. What is the lowest value for  $V_0$ ?
- 3. How much I<sub>O</sub> changes when V<sub>O</sub> changes 1V?





$$I_{2} = I_{REF} \frac{\left(W/L\right)_{2}}{\left(W/L\right)_{1}}$$

$$I_{3} = I_{REF} \frac{\left(W/L\right)_{3}}{\left(W/L\right)_{1}}$$

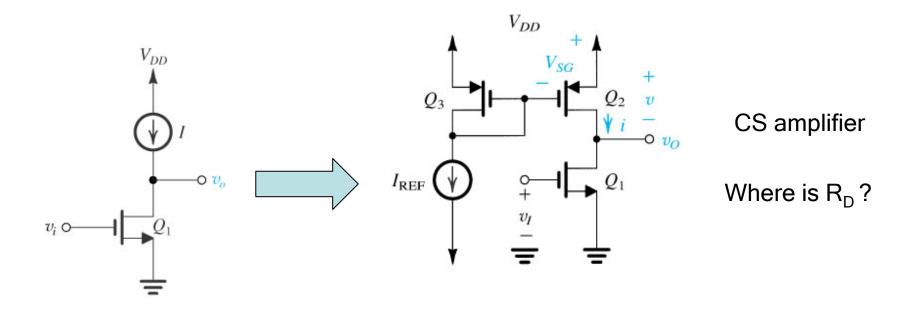
$$I_{3} = I_{REF} \frac{\left(W/L\right)_{3}}{\left(W/L\right)_{1}}$$

$$I_3 = I_4$$

$$I_5 = I_4 \frac{\left(W/L\right)_5}{\left(W/L\right)_4}$$

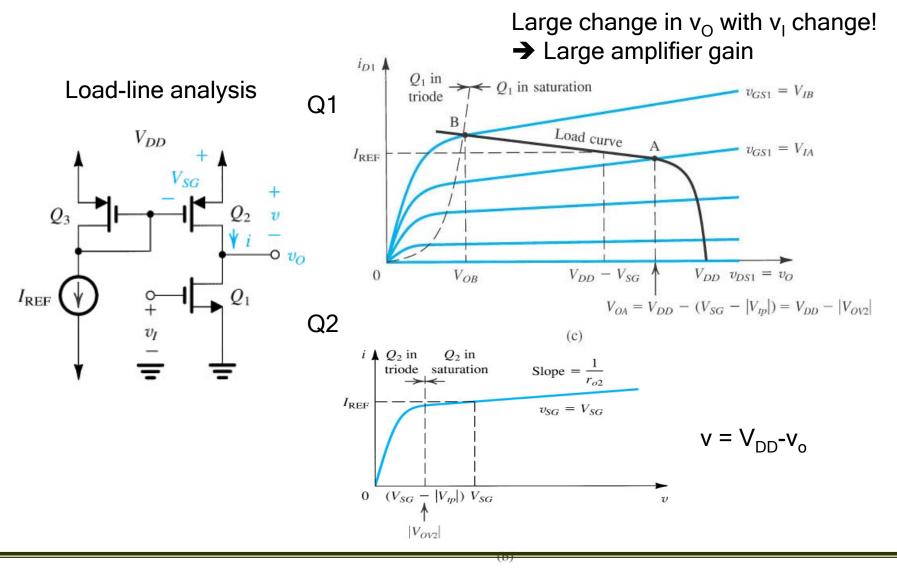
Current-steering circuits, current source (Q<sub>5</sub>), current sink (Q<sub>2</sub>)

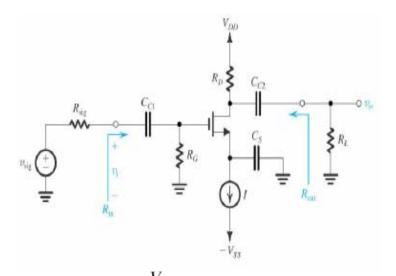




Current mirror as a resistor → Active load

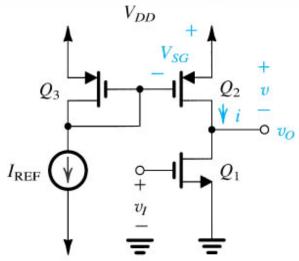
(Remember Q<sub>2</sub> has r<sub>O)</sub>





Gain for CS amplifier with R<sub>D</sub>:

$$-g_{m}\left(r_{O} \parallel R_{D} \parallel R_{L}\right)$$



Gain for CS amplifier with PMOS current mirror

$$-g_{m} (r_{O1} || r_{O2} || R_{L})$$

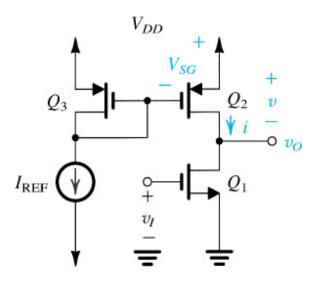
PMOS current mirror provides large "Drain" resistance (Active Load) as well as bias current!

→ Good for IC!

#### Example 6.8

$$\begin{split} &V_{DD}\text{=}3V\text{, }V_{tn}\text{=}|V_{tp}|\text{=}0.6V\text{, }k_{n}\text{'}\text{=}200\mu\text{A}/V^{2}\text{, }k_{p}\text{'}\text{=}65\mu\text{A}/V^{2}\text{,}\\ &L\text{=}0.4\mu\text{m}\text{, }W\text{=}4\mu\text{m}\text{, }V_{An}\text{=}20V\text{, }|V_{Ap}|\text{=}10V\text{, }I_{REF}\text{=}100\mu\text{A}\text{.} \end{split}$$

- 1. What is the small-signal voltage gain,  $v_O/v_I$ ?
- 2. What is the maximum  $v_0$  for which the above is valid?



1. 
$$A_{v} = -g_{m1}(r_{o1} || r_{o2})$$

$$g_{m1} = \sqrt{2k'_{n}} \left(\frac{W}{L}\right)_{1} I_{REF} = \sqrt{2 \times 200 \times \frac{4}{0.4} \times 100} = 0.63 \,\text{mA/V}$$

$$r_{o1} = \frac{V_{An}}{I_{D1}} = \frac{20 \,\text{V}}{0.1 \,\text{mA}} = 200 \,\text{k}\Omega$$

$$r_{o2} = \frac{|V_{Ap}|}{I_{D2}} = \frac{10 \,\text{V}}{0.1 \,\text{mA}} = 100 \,\text{k}\Omega$$

$$\therefore A_{D2} = -0.63 \,\text{(mA/V)} \cdot (200 \,|| \, 100) (\text{k}\Omega) = -42$$

2. For Q<sub>3</sub>, 
$$I_{REF} = \frac{1}{2}k_{p}\left(\frac{W}{L}\right)_{3}\left(V_{SG} - \left|V_{tp}\right|\right)^{2}\left(1 + \frac{V_{SD,3}}{\left|V_{Ap}\right|}\right)$$

$$100 = \frac{1}{2} \times 65\left(\frac{4}{0.4}\right)\left(V_{SG} - 0.6\right)^{2}\left(1 + \frac{V_{SG}}{10}\right)$$

$$\therefore V_{SG} = 1.13V$$

For 
$$v_{O,\text{max}}$$
,  $V_{SD2,\text{min}} = V_{SG} - |V_{tp}| = 1.13 - 0.6 = 0.53V$   

$$\therefore v_{O,\text{max}} = V_{DD} - V_{SD2,\text{min}} = 2.47V$$

Homework: Do your design project: Part 1 and 2 (No need to hand it in)

