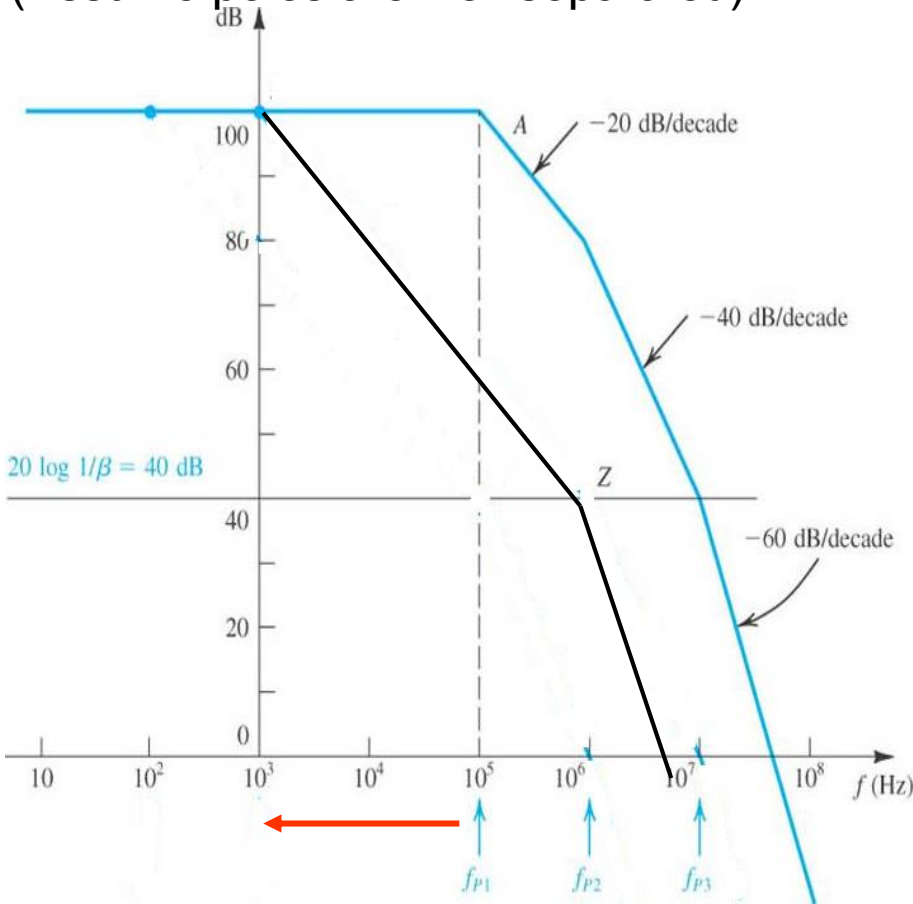


# Lect. 14: Frequency Compensation

Is amplifier having below magnitude Bode plot stable for feedback having  $\beta$ ?  
(Assume poles are well separated)



Remember Phase  $[\beta A(s)] > -180$  deg  
when  $|\beta A(s)| = 1$

-180 deg phase point occurs  
on -40dB/dec segment of  $|A|$

→ If  $|A|$  intersects  $20 \log(1/\beta)$   
with -20dB/decade slope, then stable

How can we make it stable?

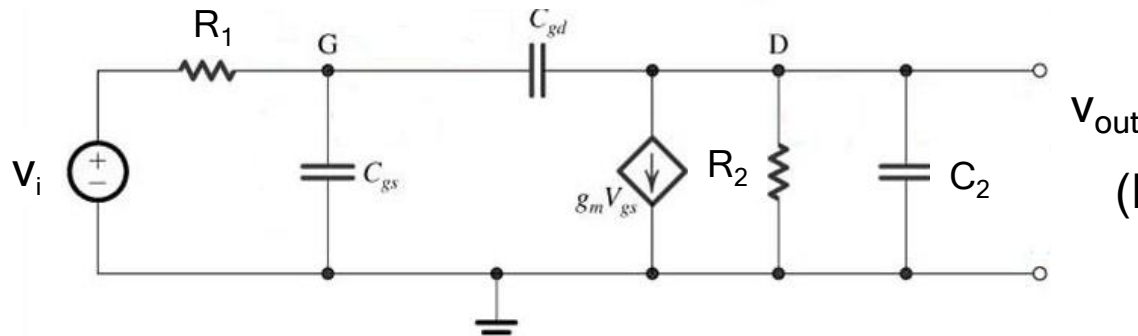
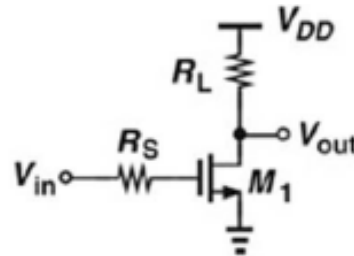
- Reduce  $\beta$
- Or move the dominant pole  
to lower frequency

→ Frequency Compensation

# Lect. 14: Frequency Compensation

How to move a pole?

Consider CS amplifier



$$(R_1 = R_S, R_2 = R_L, C_2 = C_{DB})$$

(From Lect. 12)

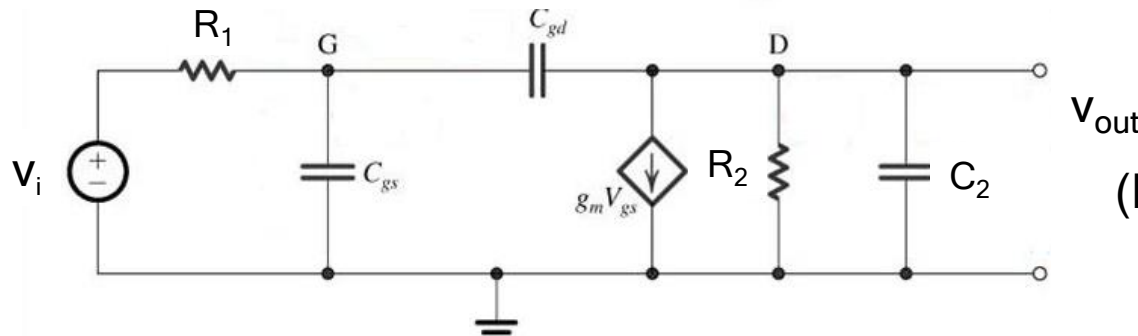
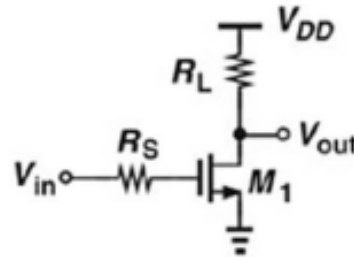
$$\frac{V_o}{V_i} = \frac{(g_m - sC_{gd})R_2}{1 + s[C_{gs}R_1 + C_2R_2 + C_{gd}(g_mR_1R_2 + R_1 + R_2)] + s^2[C_{gs}C_2 + C_{gd}(C_{gs} + C_2)]R_1R_2}$$

$$\omega_{P1} \sim \frac{1}{C_{gd}g_mR_2R_1} \quad \omega_{P2} \sim \frac{g_mC_{gd}}{C_{gs}C_2 + C_{gd}(C_{gs} + C_2)}$$

# Lect. 14: Frequency Compensation

How to move a pole?

Consider CS amplifier



$$(R_1 = R_S, R_2 = R_L, C_2 = C_{DB})$$

$$\omega_{P1} \sim \frac{1}{C_{gd} g_m R_2 R_1} \quad \omega_{P2} \sim \frac{g_m C_{gd}}{C_{gs} C_2 + C_{gd} (C_{gs} + C_2)}$$

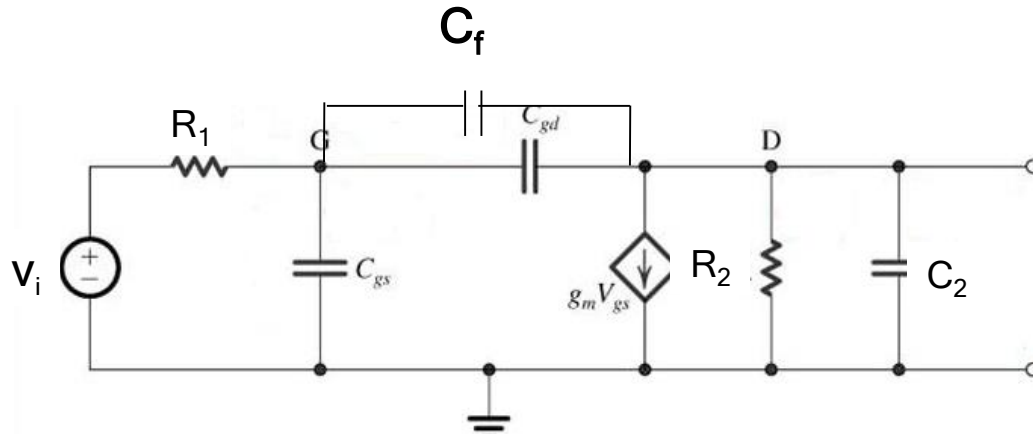
Which is the dominant pole?

Due to  $R_1$  and Miller effect of  $C_{gd}$

How can we move  $\omega_{p1}$  to lower frequency without changing the circuit too much?

# Lect. 14: Frequency Compensation

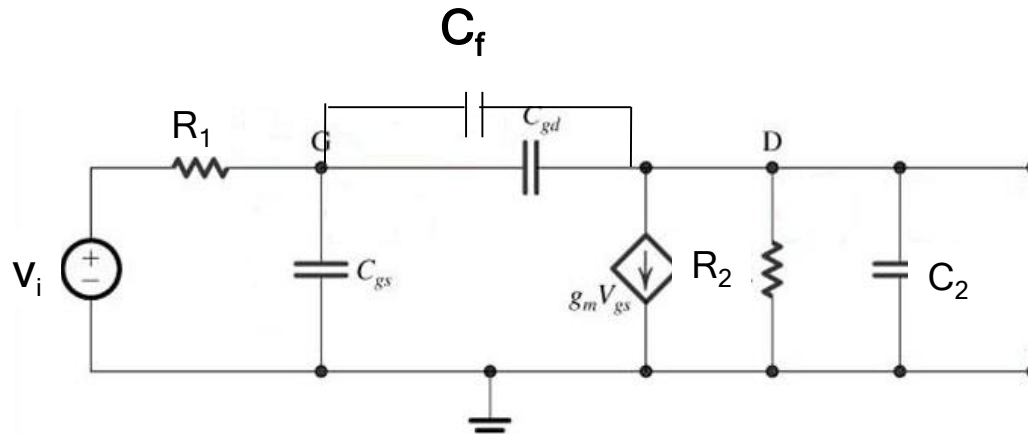
Add a feedback capacitor,  $C_f$ , ( $\gg C_{gd}$ ) between G and D



$$C_{gd} \rightarrow C_{gd} + C_f$$

$$\omega_{P1} \sim \frac{1}{C_{gd} g_m R_2 R_1} \rightarrow \frac{1}{(C_{gd} + C_f) g_m R_2 R_1} \sim \frac{1}{C_f g_m R_2 R_1}$$

# Lect. 14: Frequency Compensation



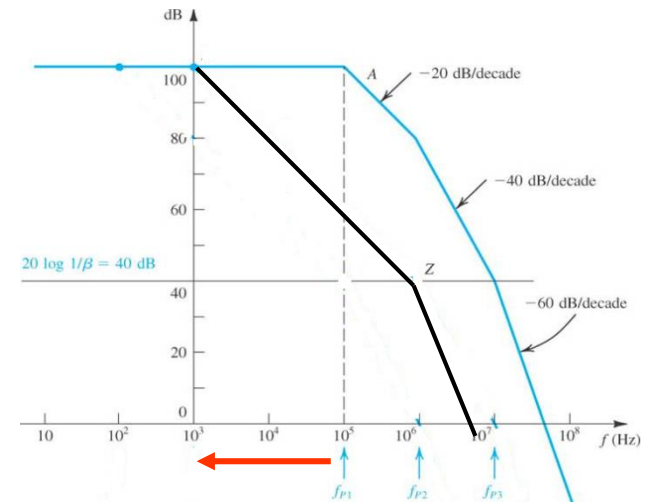
Addition of  $C_f$  between G and D

Move  $\omega_{p1}$  to lower frequency

→ More phase margin: Safer for feedback

(Lag compensation)

→ Reduces bandwidth



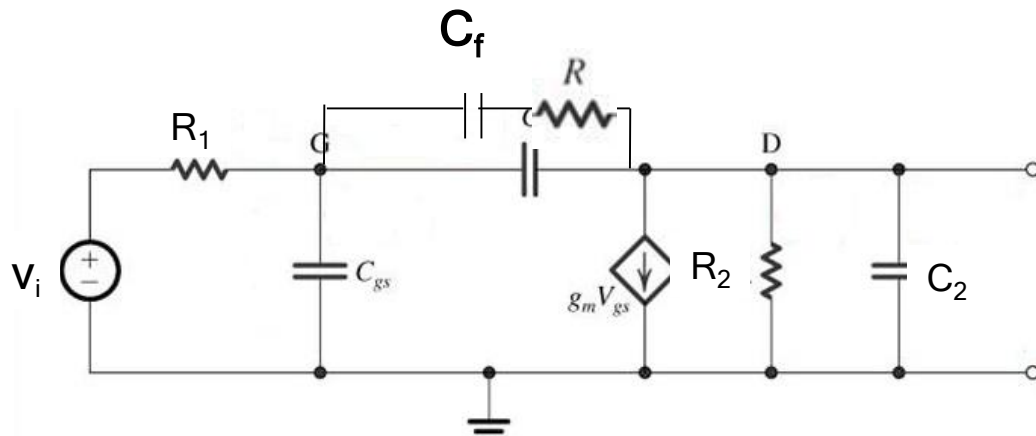
# Lect. 14: Frequency Compensation

$$\frac{V_o}{V_i} = \frac{(g_m - sC_{gd})R_2}{1 + s[C_{gs}R_1 + C_2R_2 + C_{gd}(g_mR_1R_2 + R_1 + R_2)] + s^2[C_{gs}C_2 + C_{gd}(C_{gs} + C_2)]R_1R_2}$$

Where is the zero?

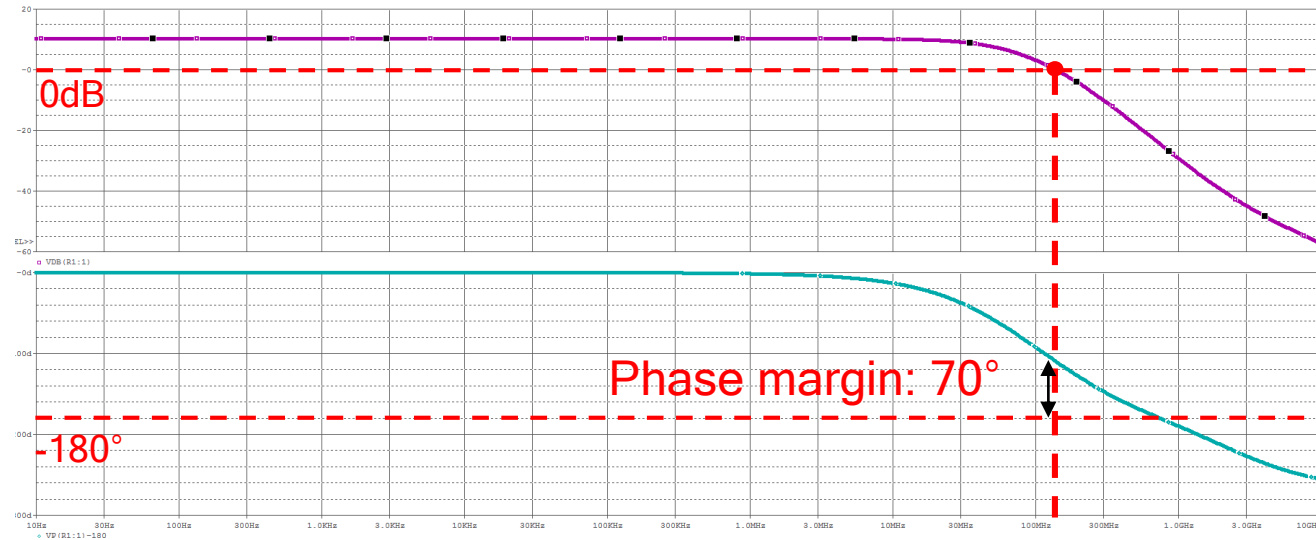
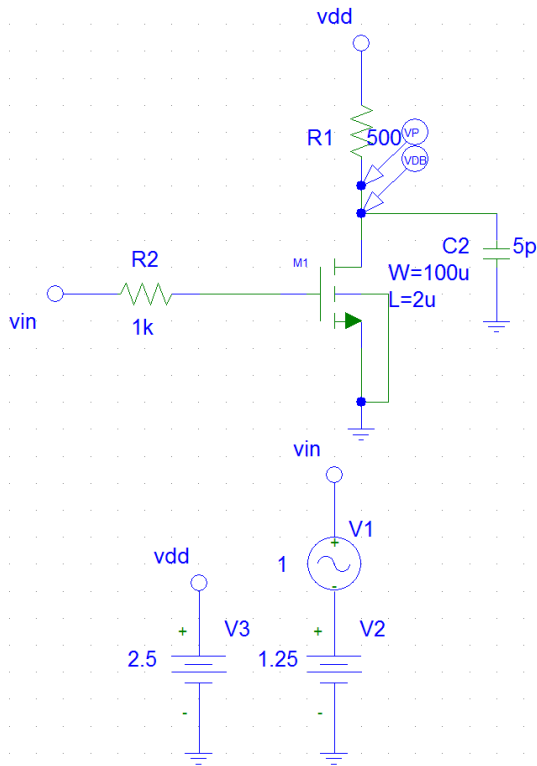
With  $C_F$  for frequency compensation?  $s = \frac{g_m}{C_F}$  (right half-plane)

Phase margin? → Need to move zero to the left half-plane

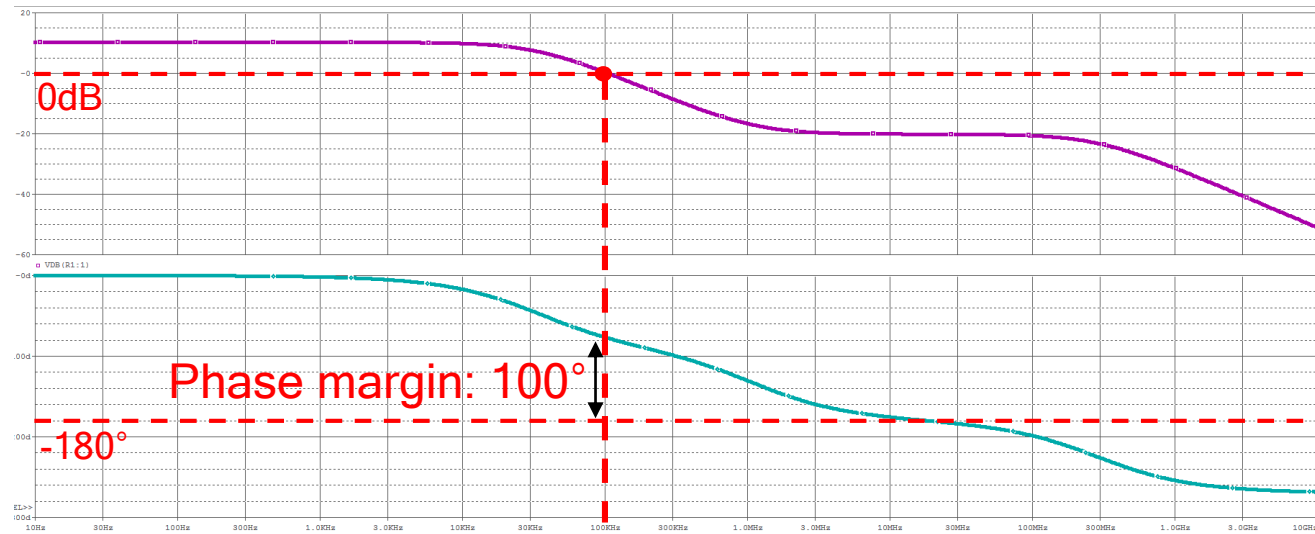
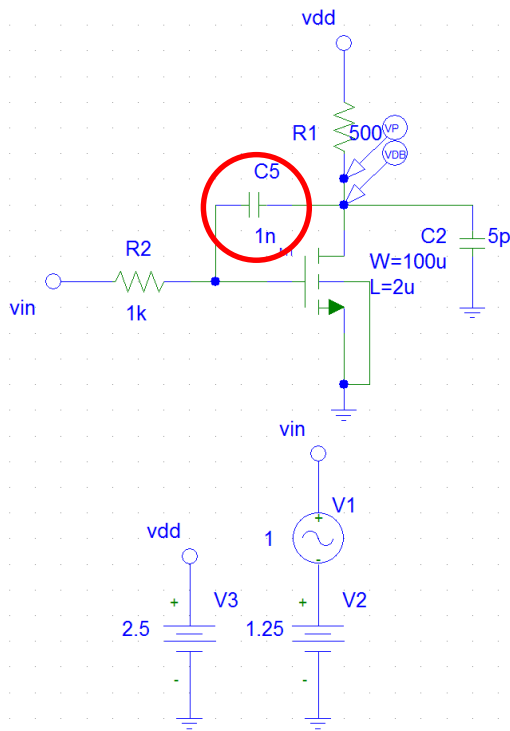


→ Discussion with simulation results

# Lect. 14: Frequency Compensation



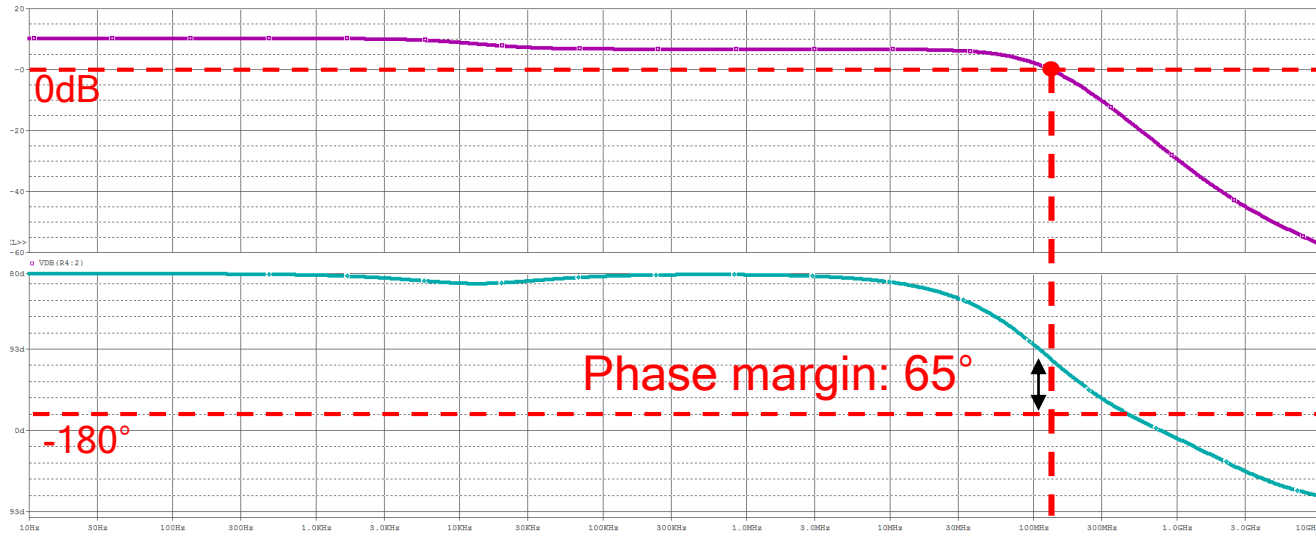
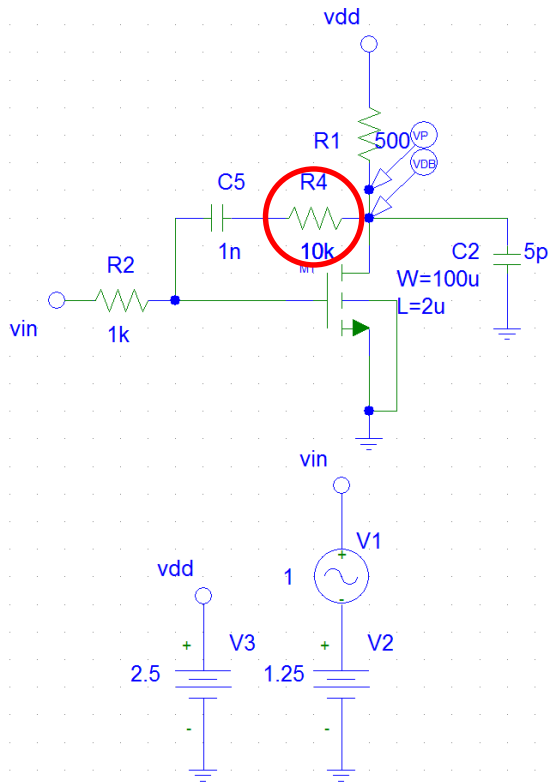
# Lect. 14: Frequency Compensation



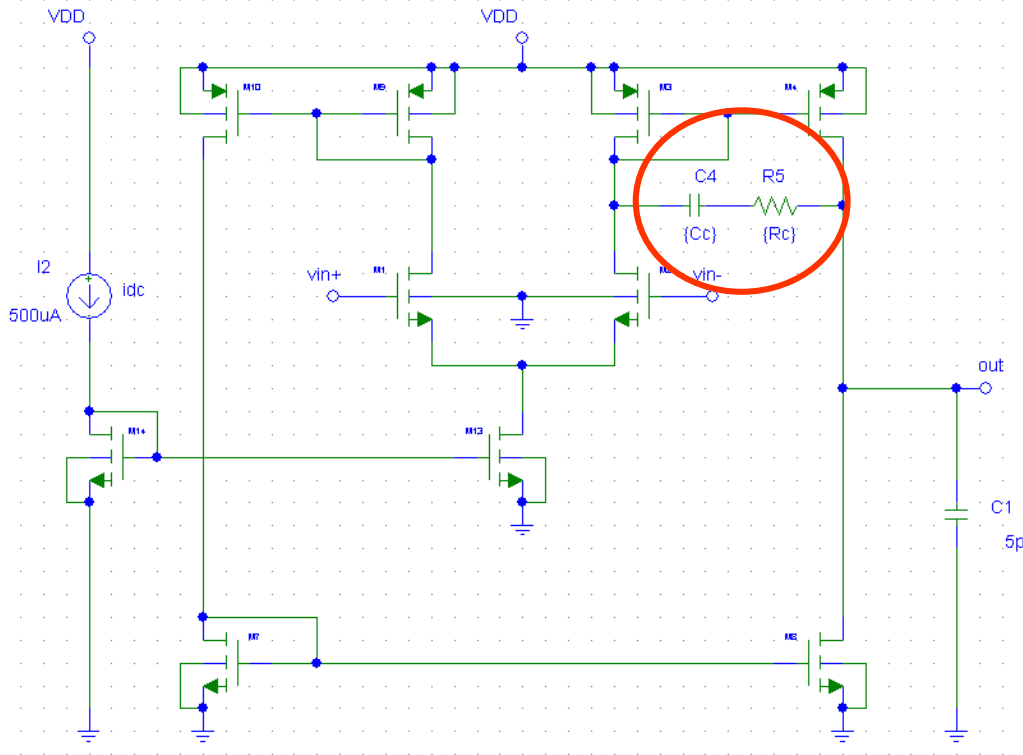




# Lect. 14: Frequency Compensation



# Lect. 14: Frequency Compensation



- Mirrored OTA Specifications

Parameter	Value
$A_v$	> 56dB
Bandwidth	> 60KHz
Phase Margin	> 65°
$V_{p-p}$	> 1.5V
Slew Rate	> 13MV/s
CMRR	> 85dB
Power Consumption	< 2.5mW

Determine R and C for the optimal bandwidth and phase margin performance

Design Project help session next Monday during class: Q/A, progress check