
High-spectral-efficiency optical modulation formats

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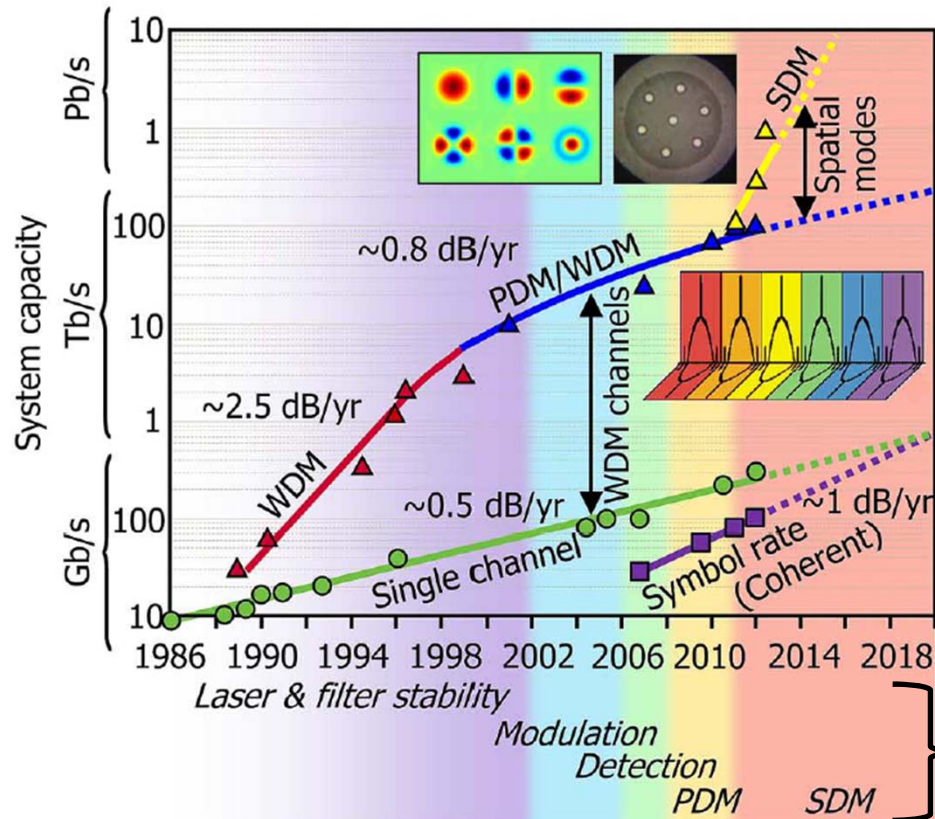
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- Introduction
- The Anatomy of a Modulation Format
- Key Trade-Offs in Choosing a Modulation Format
- Conclusion

Introduction

- Communication system: grows exponentially
- Demand for communication bandwidth
: wavelength-division multiplexed (WDM) optical transmission systems
- Researched, developed since the early 1990s
- Research experiments → commercial products follows in 5 years

Growth of optical communication system

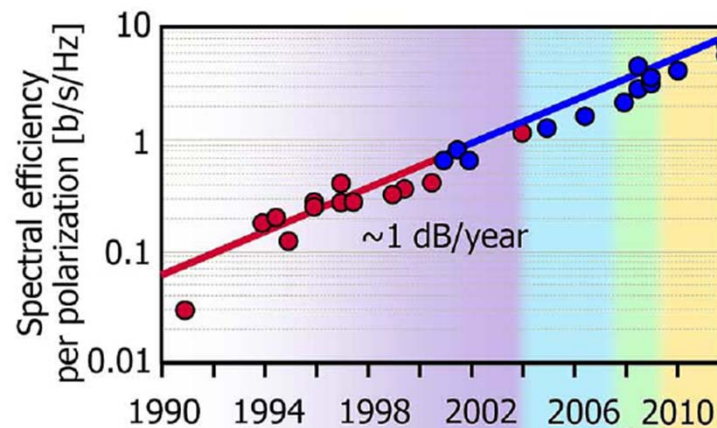


Evolution of various bit rates

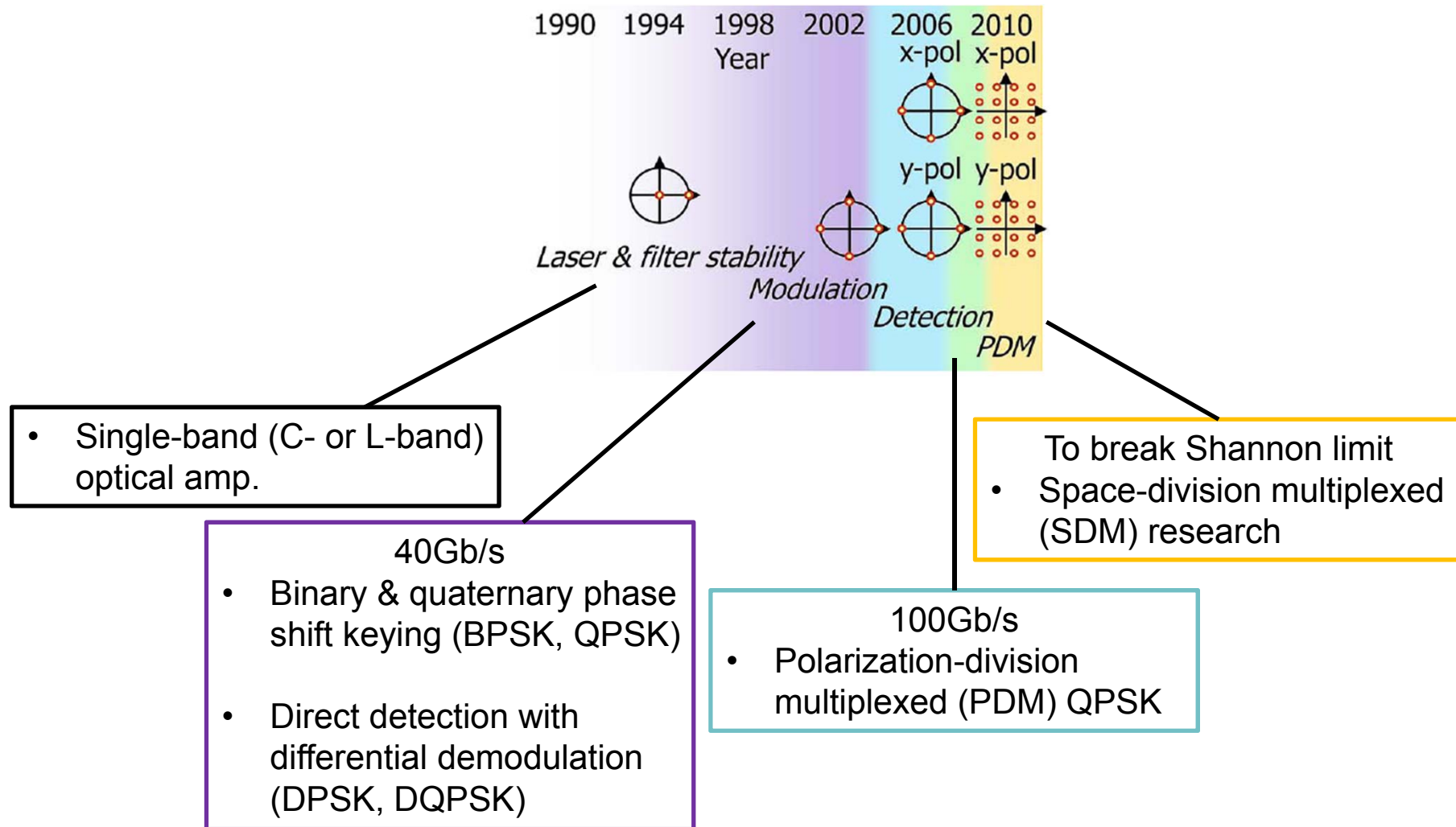
- Single-channel bit rates : 0.5 dB/year
- Aggregate per-fiber capacities : **2.5 dB/year**
- Rapid advances in optoelectronic device technologies

“Optical and electronic bandwidths had met”

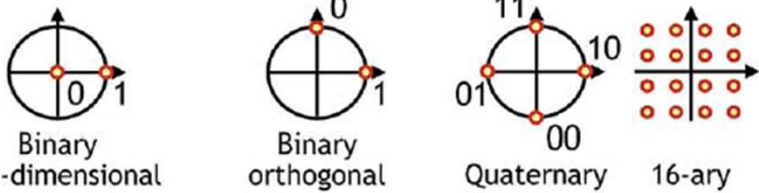
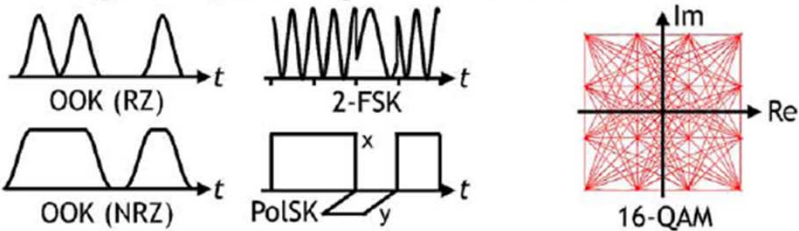
- Advance in optical & electronic & optoelectronic device technologies
- Laser reached GHz frequency stabilities (early 2000s)
- Optical filter: BW for 50-GHz WDM channel spacings
- Efforts on increasing “spectral efficiencies”
 - : To pack more information into the limited BW (~5-THz)



Development of optical modulation



Digital communication & Structure of Language

<i>Language</i>	<i>Digital communications</i>
<p><i>Alphabets of letters</i></p> <p>{A,B,C,...,Z}, {α,β,γ,...,ω}, {0,1,2,...,9}</p>	<p><i>Symbol alphabets (constellations)</i></p>  <p>Binary one-dimensional Binary orthogonal Quaternary 16-ary</p>
<p><i>Analog letter representations</i></p> <p>'A' → A, <i>A</i>, A, <i>A</i>, A, ...</p>	<p><i>Analog waveform representations</i></p>  <p>OOK (NRZ) OOK (RZ) 2-FSK PolSK 16-QAM</p>
<p><i>Letters arranged in series</i></p>	<p><i>One symbol transmitted per symbol period</i></p>
<p><i>Redundancy in words or sentences</i></p> <p>'language' or 'lanyage' → 'language'</p>	<p><i>Error correcting codes</i></p> <p><i>Overhead in time (forward error correction, FEC) or in symbol alphabet (coded modulation)</i></p>
<p><i>Synonym expressions</i></p> <p>(ex: use 'ponder' instead of 'think' to avoid confusion with 'sink')</p>	<p><i>Line coding</i></p> <p><i>Overhead in time or in symbol alphabet</i></p> <p>(ex: '11011' → {+1,+1,0,-1,-1}: 'Duobinary')</p>

Notation

$\{a_k\}$: discrete communication symbols (constellation)

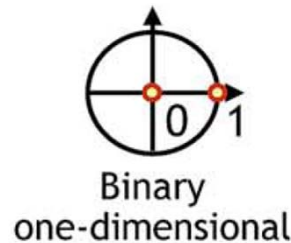
$\{x_k(t)\}$: a set of analog waveforms (corresponds to each symbols)

R_S : Sequentially transmitted symbol rate (Symbol period $T_S = 1/R_S$)

Transmit waveform $s(t) = \sum_k x_k(t - kT_S)$

M : Constellation size (number of available alphabet letters)
: Each symbol conveys $\log_2 M$ bits of information

Bit rate $R_B = R_S \log_2 M$

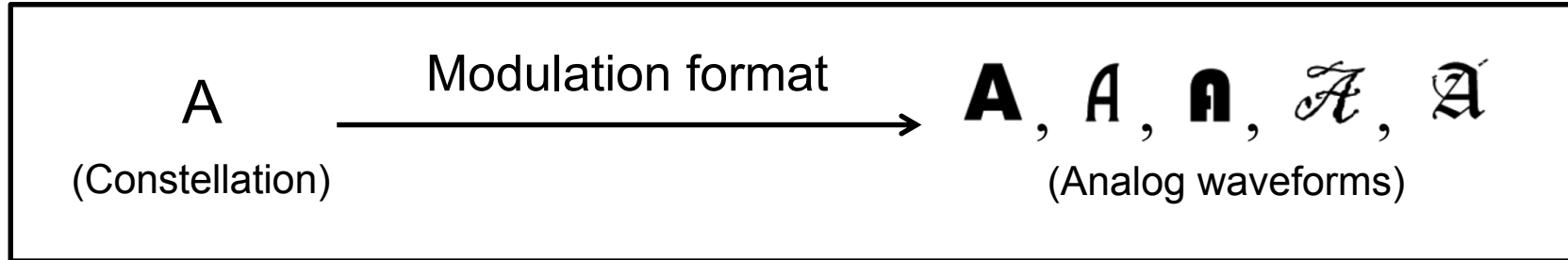


Ex) Simple binary symbol

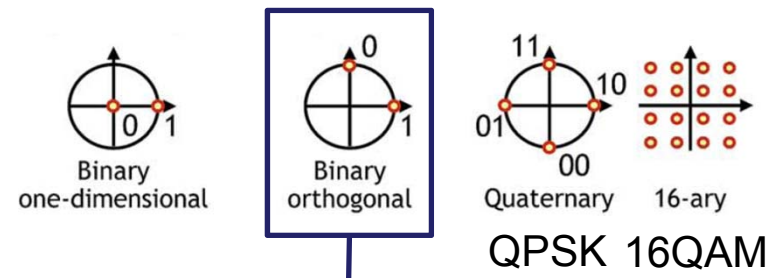
$M=2$

Symbols: Sending no pulse &
sending a pulse

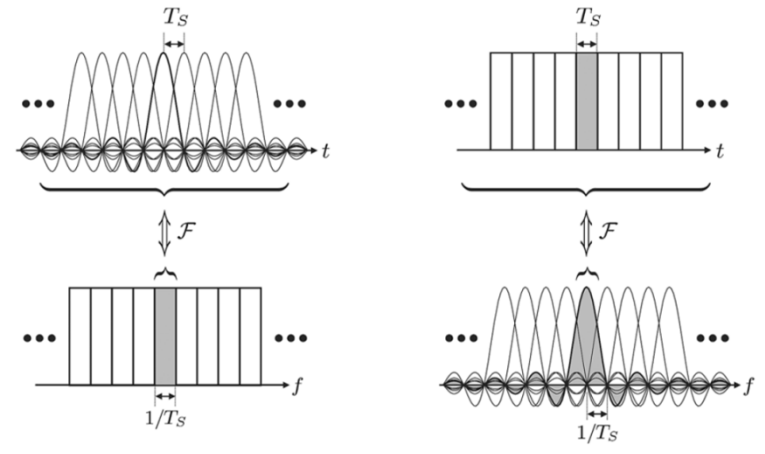
Modulation format



Examples of constellation



Condition of orthogonal symbols
:No inter-symbol interference

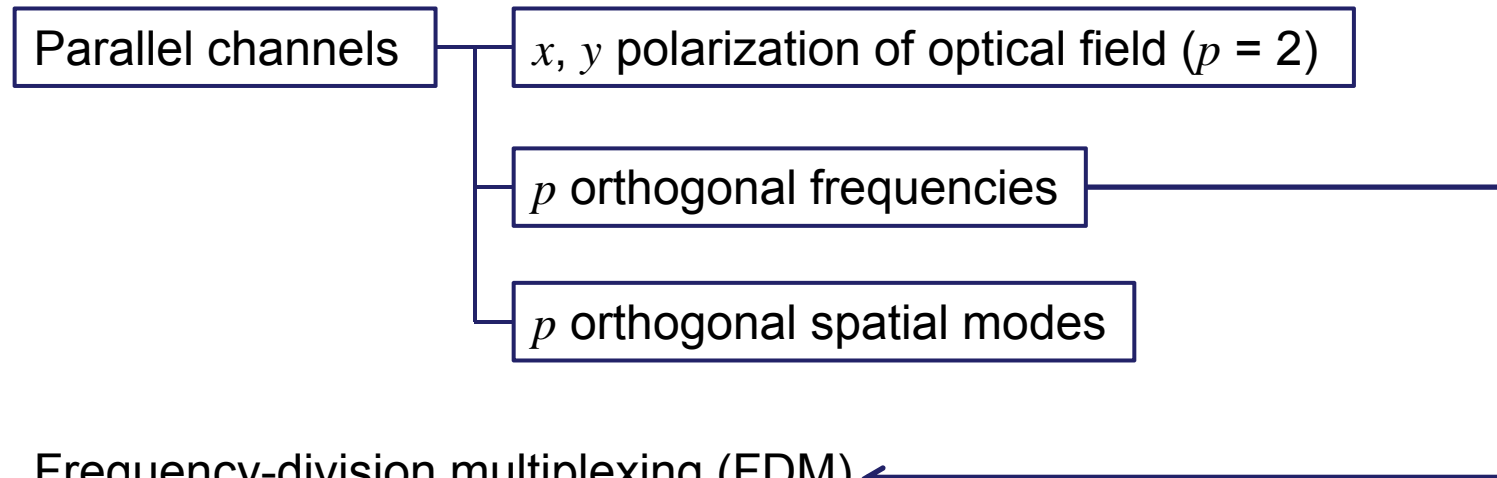


$$\int_{-\infty}^{\infty} dt \iint_{-\infty}^{\infty} d\vec{r} \vec{x}_1(t, \vec{r}) \cdot \vec{x}_2^*(t, \vec{r}) =$$

$$\int_{-\infty}^{\infty} df \iint_{-\infty}^{\infty} d\vec{r} \vec{X}_1(f, \vec{r}) \cdot \vec{X}_2^*(f, \vec{r}) = 0$$

Multiplexing

$R_B = pR_S \log_2 M$: the aggregate bit rate of multiplexed system
(p number of parallel channels)



Frequency-division multiplexing (FDM) ←
- Example in EM wave: radio system (channel selection for frequency)

Coding

(Recall: Table 1)

<i>Redundancy in words or sentences</i> 'laguage' or 'lanyage' → 'language'	<i>Error correcting codes</i> <i>Overhead</i> in time (forward error correction, FEC) or in symbol alphabet (coded modulation)	: Forward error correction
<i>Synonym expressions</i> (ex: use 'ponder' instead of 'think' to avoid confusion with 'sink')	<i>Line coding</i> <i>Overhead</i> in time or in symbol alphabet (ex: '11011' → {+1,+1,0,-1,-1}: 'Duobinary')	: Line coding

→ Inject redundancy in digital communication

Line rate: gross channel bit rate including all coding redundancy

Code rate R_c (< 1): ratio of information bit rate to line rate

Coding overhead $\text{OH} = (1 - R_c)/R_c$

(OH ~ 7% for standard fiber-optic communication system)

DAC resolution

(Recall: multiplexed system)

$$R_B = pR_s \log_2 M$$

Linear dependence on R_s

Log dependence on M

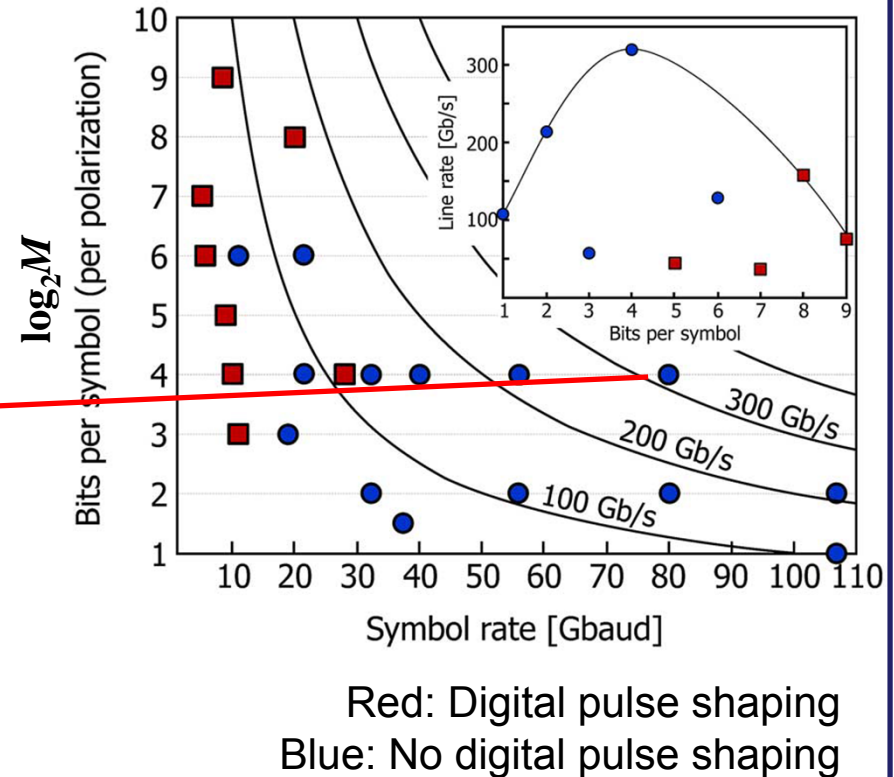
Optimized point ←
 $M = 16$ (320 Gb/s line rates)
 (16-QAM as modulation format)

Minimum DAC resolution

$$\log_2 \sqrt{M} \text{ bits}$$

Optimization: $M > 16$ for CMOS-integrated DAC+DSP ASIC solution

Experimentally measured performance



ADC resolution

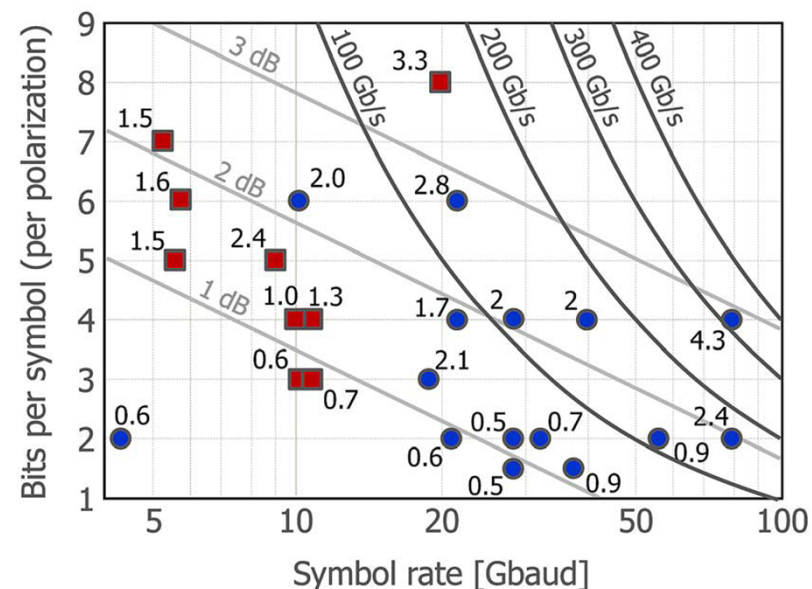
ADC resolution: specified in terms of **ENoB** (effective number of bits)

M	$\log_2(M)$	\sqrt{M}	$\log_2(\sqrt{M})$	ENoB [67]
4	2	2	1	~4
16	4	4	2	~5
64	6	8	3	~6
256	8	16	4	~7

+3 bits →

1-dB receiver sensitivity penalty
pre-FED bit error ratio (typically 10^{-3})

→ 3 bits more than $\log_2 \sqrt{M}$



Transmitter/receiver sensitivity penalty
Gap between experimentally achieved and theoretically possible SNR
(BER of 10^{-2})

Digital filter size

Linear optical impairments

: can be compensated by digital filters in receiver's DSP

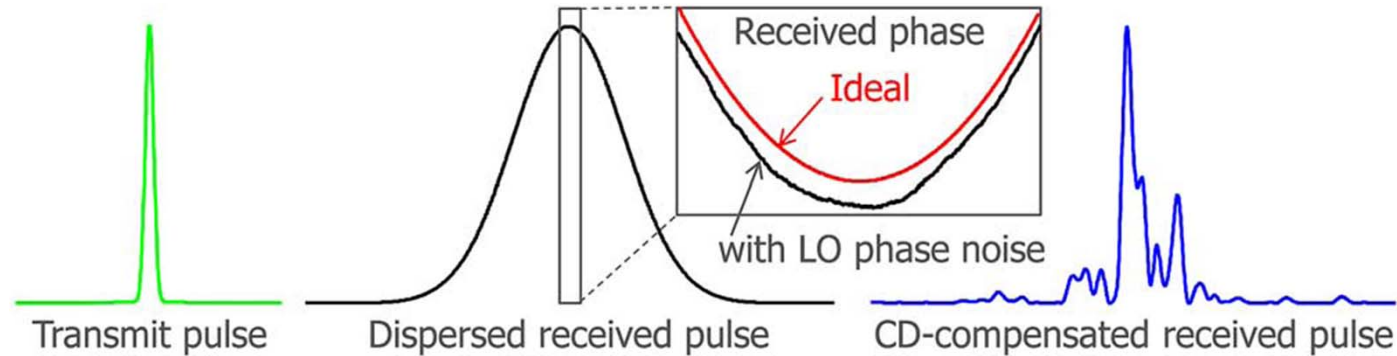
- Chromatic dispersion (CD)
- Polarization-mode dispersion (PMD)
- Etc...

CD can be compensated using a filter with inverse phase profile
Ex. 2000 km of standard single-mode fiber
→ CD compensation capability of 34 ns/nm at ~30 GBaud

Length of filter's impulse response $\sim 0.032 \cdot CD_{[\text{ns/nm}]} \cdot R_S^2_{[\text{GBaud}]}$

(Adjacent-pulse overlap: due to dispersive pulse broadening)
→ scales quadratically with symbol rate

Laser phase noise



Phase noise → degrades detection performance

- Random phase fluctuation of signal & local oscillator light
- Pattern-dependent phase perturbations (due to fiber nonlinearities)

More sensitive in higher-order modulation formats

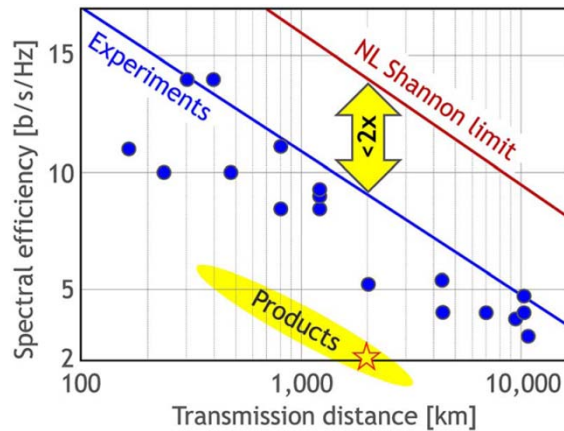
Spectral Efficiency vs. Noise

Independent of single-channel interface rates & constellation size

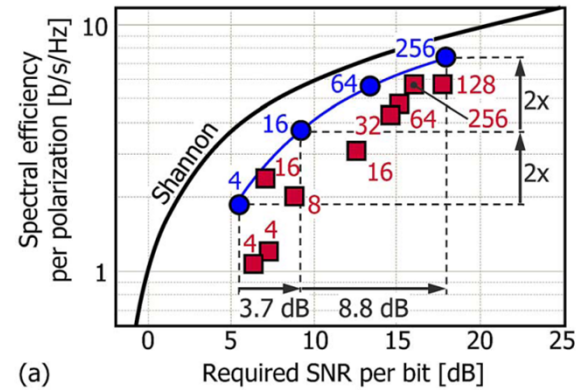
Trade between:
Spectral efficiency & System noise

(In linear regime) ←
Shannon limit: linear, additive white
Gaussian noise channel

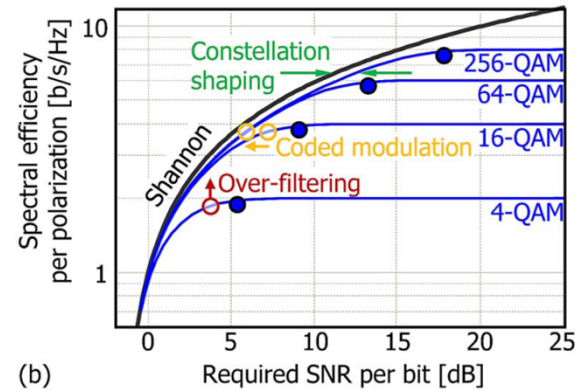
(Impact of advanced coding) ←



Trade between:
Spectral efficiency & Transmission reach



(a)

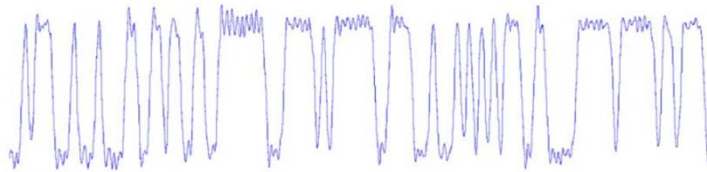


(b)

Spectral efficiency & pulse shaping

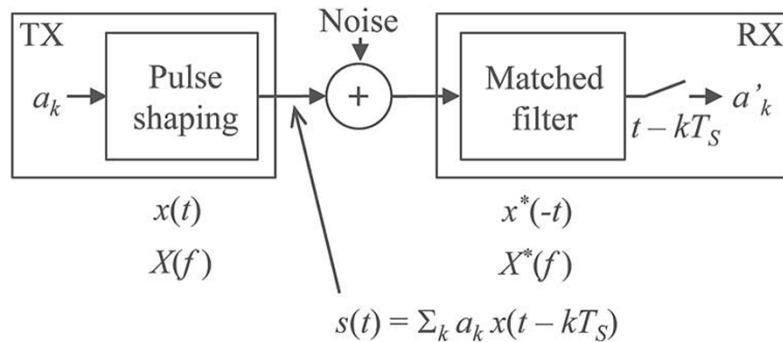
Choice of analog transmit waveforms is important aspect

- Electronic multiplexers (to generate binary drive signals)
: Output determine exact pulse shape

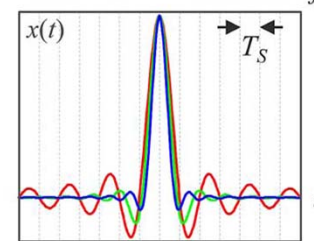
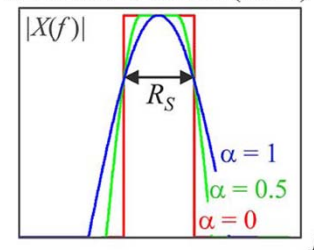


Non-return-to-zero (NRZ) waveform
: Significant amount of **non-linear ISI**
Cannot be removed by linear equalization

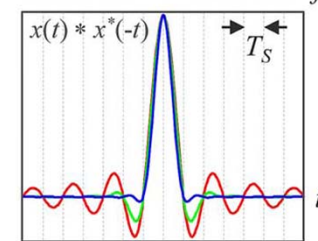
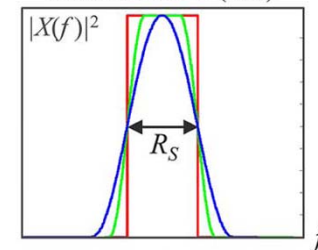
Best solution: pulse shaping



Root raised cosine (RRC)



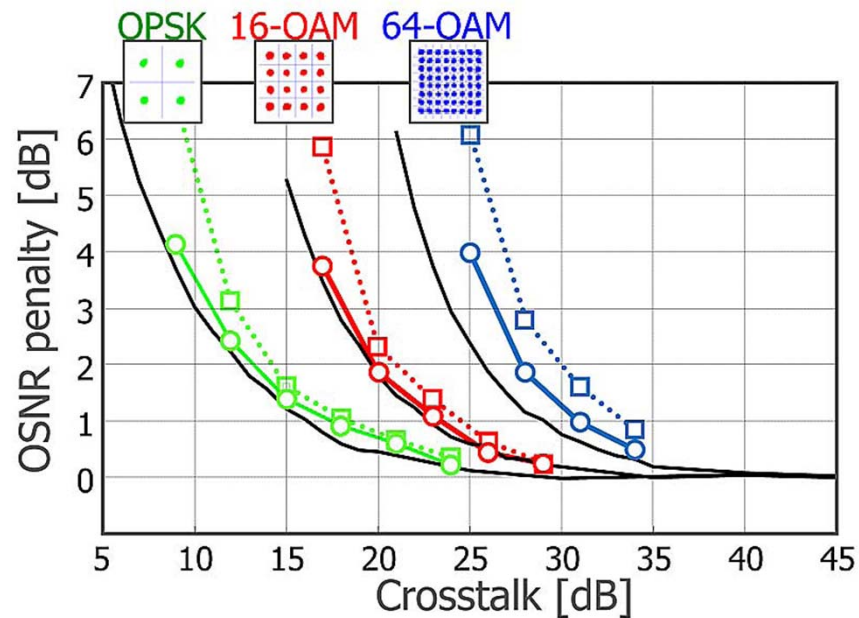
Raised cosine (RC)



Crosstalk tolerance

Crosstalk between individual channels

- WDM crosstalk: among neighboring WDM channels
- In-band crosstalk: signals along same wavelength slot

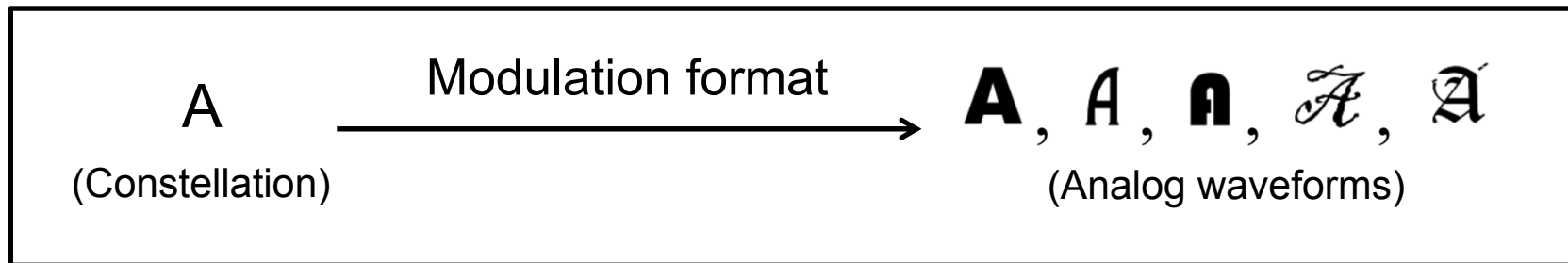


SNR penalty vs. Crosstalk (BER of 10^{-3})

- Higher-order modulation format
→ Crosstalk \uparrow
- High power required to ignore crosstalk

Conclusion

- Structure of optical modulation formats
 - Constellation (Digital)
 - Pulse shaping (Analog)



- Trade-off between symbol rate, constellation size, and pulse shaping effect
 - Investigate optimal point of communication performance
($R_B = pR_S \log_2 M$)