Lect. 5: Boundary Conditions (Cheng 7–5)

- ✓ Boundary Conditions: Constraints on E,H fields at a boundary
 - → Each Maxwell's Eq. provides one constraint on E or H.



$$D = \rho$$
$$D_{1,n} - D_{2,n} = \rho_s$$

 $\varepsilon_1 E_{1,n} - \varepsilon_2 E_{2,n} = \rho_s$





- ✓ Boundary Conditions: Constraints on E,H fields at a boundary
 - → Each Maxwell's Eq. provides one constraint on E or H.



$$\nabla \cdot \overline{B} = 0$$
$$B_{1,n} - B_{2,n} = 0$$
$$\mu_1 H_{1,n} - \mu_2 H_{2,n} = 0$$



E&M 2 (16/1)

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$$\nabla \times \overline{H} = \overline{J} + \frac{\partial \overline{D}}{\partial t}$$
$$H_{1,t} - H_{2,t} = J_s$$



E&M 2 (16/1)

Boundary Conditions are 2–D Maxwell's Eqs.

$$\varepsilon_{2}, \mu_{2} \qquad \varepsilon_{1}, \mu_{1} \qquad \nabla \cdot \overline{D} = \rho \qquad D_{1,n} - D_{2,n} = \rho_{s} \Leftrightarrow \varepsilon_{1} E_{1,n} - \varepsilon_{2} E_{2,n} = \rho_{s} \\ \nabla \times \overline{E} = -\frac{\partial \overline{B}}{\partial t} \qquad E_{1,t} - E_{2,t} = 0 \\ \nabla \cdot \overline{B} = 0 \qquad B_{1,n} - B_{2,n} = 0 \Leftrightarrow \mu_{1} H_{1,n} - \mu_{2} H_{2,n} = 0 \\ \nabla \times \overline{H} = \overline{J} + \frac{\partial \overline{D}}{\partial t} \qquad H_{1,t} - H_{2,t} = J_{s} \end{cases}$$

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$$\begin{array}{l}
\varepsilon, \mu \\
\sigma = 0 \\
\overline{E} = \overline{H} = 0
\end{array}$$

Characteristics of E, H field on the surface of a perfect conductor?



