## Quiz 2

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E\&M II
Prof. Woo-Young Choi

## Name:

## Prob. 1(4)

A plane wave is propagating in a medium having $\varepsilon=2 \varepsilon_{0}$ and $\mu=\mu_{0}$ and its H -field is characterized as $\bar{H}=\bar{y} H_{0} \exp (j x-j z) \exp (\omega t)$, where $H_{0}$ is a real constant. $\mathrm{x}, \mathrm{z}$ are in meter and $\omega$ is in radian/sec.
(a)(1) In what direction in the $x-z$ plane does this wave propagate? Draw an arrow in the $x-z$ plane indicating the propagation direction and express the angle the arrow makes with the $x$-axis.
(b)(1) What is the numerical value for $\omega$ ?
(c)(2) What is the E-field of this wave? Give your answer in terms of parameters given in this problem.

## Prob. 2 (2)

Consider an electromagnetic wave having $\bar{H}=\bar{x} \exp (-j z) \exp (j \omega t)$.
(a)(1) What is the polarization of this EM wave?
(b)(1) Show that this wave can be expressed by a sum of two circular polarized wave.

## Prob. 3 (2)

A plane wave having with frequency $\omega$ is normally incident from vacuum into a highly conductive material as shown below.
(a)(1) What is the penetration depth for the wave in region 2? Give your answer in terms of $\omega, \mu$ and $\sigma$.
(b)(1) What is the phase difference between E -field and H -field $((\angle \bar{E}-\angle \bar{H})$ ?

Give your answer in degree with the correct sign.

$$
\begin{array}{c|ccc}
\varepsilon_{o}, \mu_{o} & \begin{array}{ll}
\mu, \sigma \gg 1 & \\
E_{i} \rightarrow & \text { Region2 } \\
\boldsymbol{E}_{t}
\end{array}
\end{array}
$$

## Prob. 4 (2)

A plasma has the plasma frequency of $\omega$ p.
(a)(1) Plot the dependence of $\beta$ (propagation constant) on $\omega$ (angular frequency) for the EM wave propagating in the plasma when $\omega>\omega_{\mathrm{p}}$
(b)(1) How does the group velocity of the EM wave change as $\omega$ increases?

