What happens when photons interact with a matter whose electron transition energies are compatible with photon energies?

For example: Electron energy levels in an hydrogen atom



According to QM, energy levels inside matter are quantized

This interaction is basis for spectroscopic characterization of materials and light light emitting devices



Consider for simplicity only two energy levels: ground state and first excited state Assume  $hv = E_2 - E_1$ 





Determine the rate for each process



 $\rho$ : photon density (spectral photon energy density)  $N_{1,2}$ : electron density at  $E_{1,2}$  $B_{12}, B_{sp}, B_{21}$ : constants



What happens at equalibrium (No net change of  $N_1$ ,  $N_2$ ,  $\rho$ )?

$$R_{12} = R_{sp} + R_{21}$$

$$B_{12} \cdot N_1 \cdot \rho = A_{21} \cdot N_2 + B_{21} \cdot N_2 \cdot \rho$$

$$\rho = \frac{A_{21}}{B_{12}} \qquad \therefore \rho(E_2 - E_1) = \frac{A_{21}}{B_{12}} + \frac{B_{21}}{B_{12}} + \frac{B$$

From another branch of physics (statistical mechanics),

electron distribution at equilibrium

$$\frac{N_2}{N_1} = \exp\left(-\frac{E_2 - E_1}{kT}\right) \xrightarrow{E_2} E_2$$

From Lect. 16, (Planck law for black-body radiation)



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Compare



For  $hv = E_1 - E_2$ , two expressions should be identical.

$$\frac{B_{21}}{B_{12}} = 1 \qquad \qquad \frac{A_{21}}{B_{12}} = \frac{8\pi h \upsilon^3}{c^3}$$

→ Einstein's A, B constants







Spontaneous emission is simulated emission due to vacuum fluctuation (QM interpretation of EM waves)



Which process is dominant at equilibrium?

Stimulated emission vs. absorption



Absorption is dominant over stimulated emission at equilibrium



Which process is dominant at equilibrium?



Almost all incident photons experience absorption

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Which process is dominant at equilibrium?

Stimulated emission vs. spontaneous emission



Spontaneous emission is dominant over stimulated emission at equilibrium



Which process is dominant at equalibrium?



Virtually all photon emission is due to spontaneous emission at equilibrium



How can we induce stimulated emission?



Make  $N_2$  larger than  $N_1$ : Break equilibrium by pumping carriers into  $E_2$ 

 $N_2 = N_1$ : transparent

 $N_2 > N_1$ : population inversion





#### Homework:

A material with two energy levels and photons are at the equilibrium state as shown

below. The photon energy,  $E_p$ , is equal to  $E_2$ - $E_1$ =100meV. Use kT=25meV.

(a) What is the expression for the stimulated emission rate?

(b) Determine the numerical value of  $\rm N_1/\rm N_2,$  the ratio between electron densities at  $\rm E_2$  and  $\rm E_1.$ 

(c) What is the percentage of photons that are due to stimulated emission?

(d) Electron are excited from E<sub>1</sub> to E<sub>2</sub> by optical pumping. If the total density of electrons in the material is N, what should be N<sub>2</sub> in order to reach the transparency condition?



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