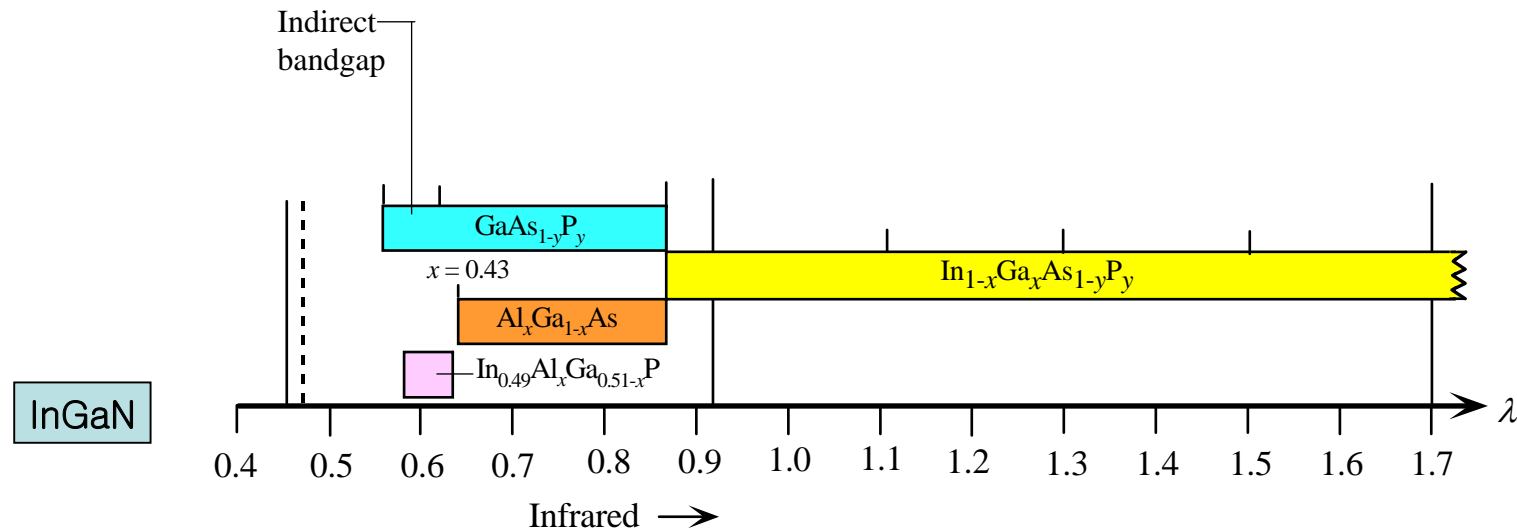


Lect. 22: Semiconductor Lasers

- Semiconductors lasers are small, cheap and very efficient

- Lasing wavelength:

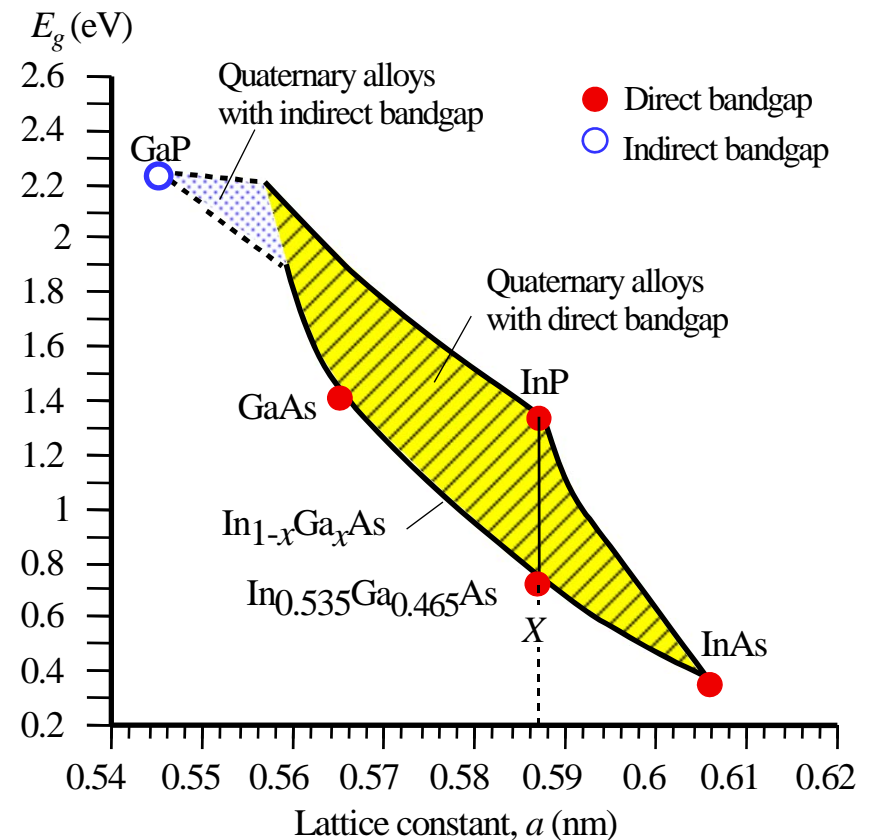
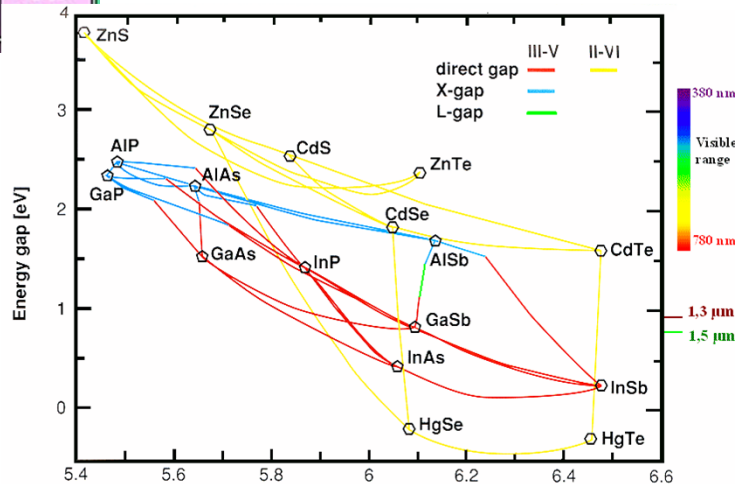
Bandgap of direct semiconductor materials (III–V compound semiconductors)



Lect. 22: Semiconductor Lasers

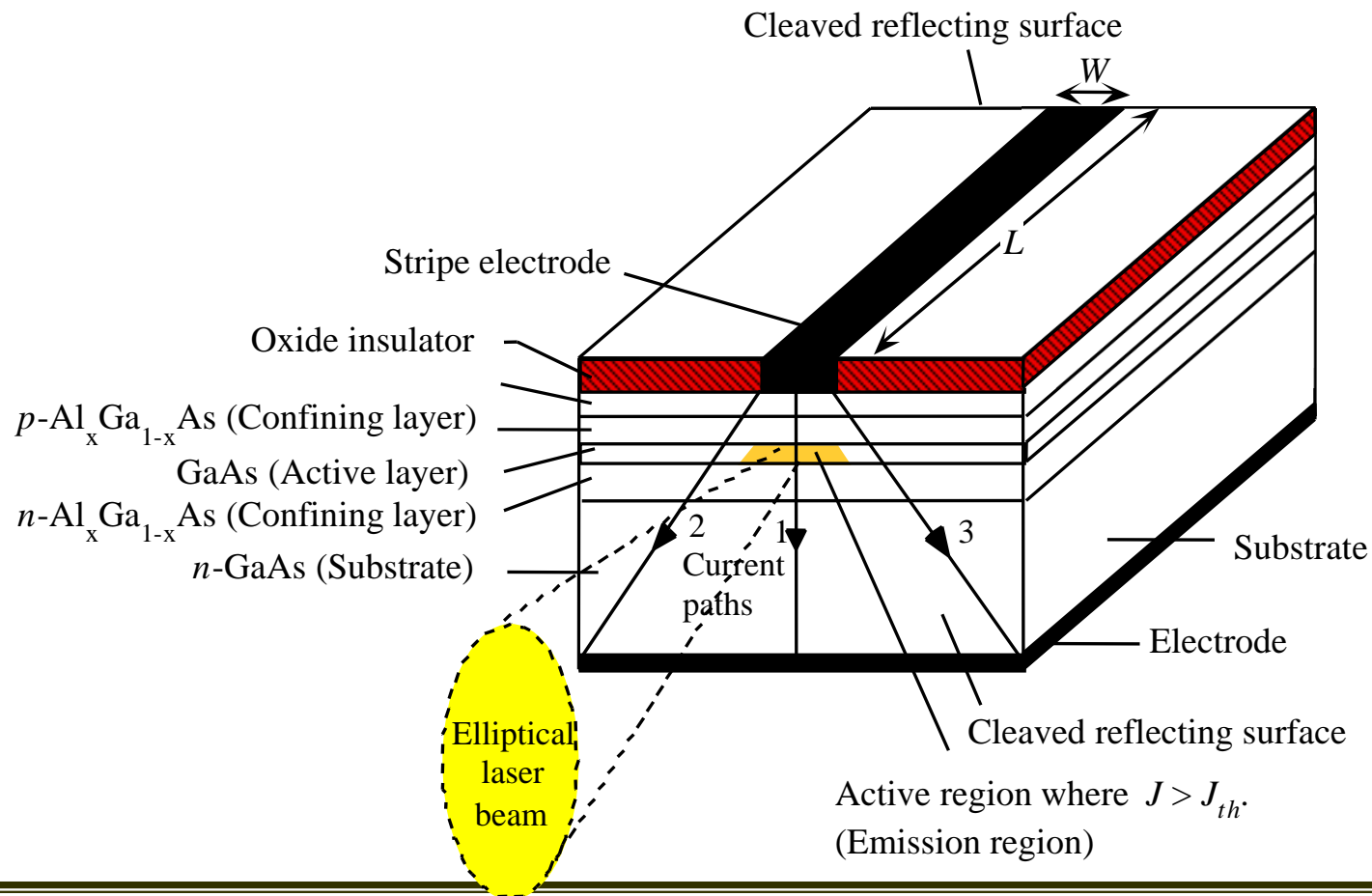
– $\text{Al}_x\text{Ga}_{1-x}\text{As}$ (ternary) and $\text{In}_{1-x}\text{Ga}_x\text{As}_{1-y}\text{P}_y$ (quaternary) material systems

	13/IIIA	14/IVA	15/VA
	5 B 10.81	6 C 12.01	7 N 14.01
	13 Al 26.98	14 Si 28.09	15 P 30.97
B	31 Ga 69.72	32 Ge 72.61	33 As 74.92
	49 In 114.8	50 Sn 118.7	51 Sb



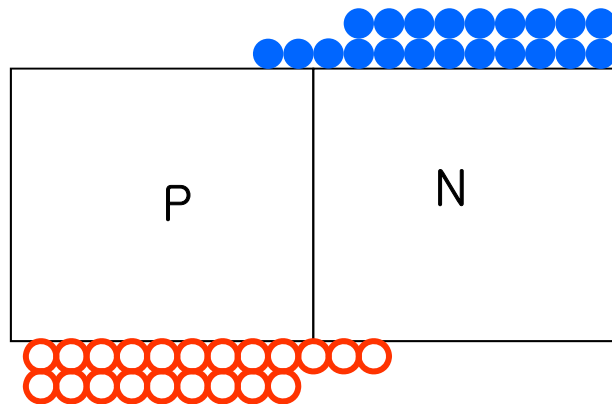
Lect. 22: Semiconductor Lasers

Semiconductor Laser Structure: PN Junction + Mirror (Cleaved Facets)



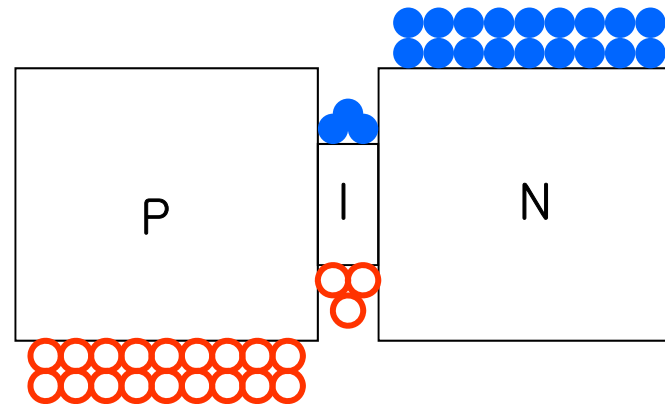
Lect. 22: Semiconductor Lasers

Efficient carrier confinement: PIN structure with large E_g for P, N regions



Injected carriers are spread-out
=> smaller density

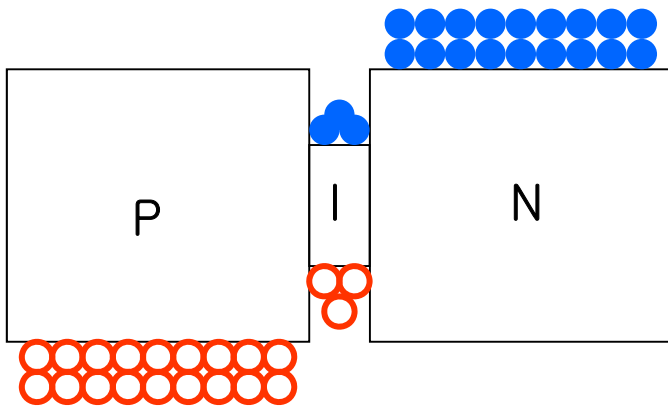
For population inversion, $\frac{N_2 \cdot P_1}{N_1 \cdot P_2} > 1$



Double heterojunction: Confinement of
Injected carriers
=> larger density

Lect. 22: Semiconductor Lasers

The Nobel Prize in Physics 2000



Double heterojunction



Zhores I. Alferov
Prize share: 1/4

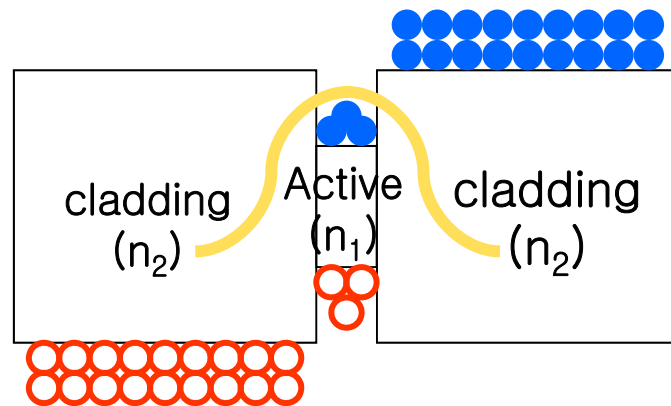


Herbert Kroemer
Prize share: 1/4

The Nobel Prize in Physics 2000 was awarded to Zhores I. Alferov and Herbert Kroemer *"for developing semiconductor heterostructures used in high-speed- and optoelectronics"*

Lect. 22: Semiconductor Lasers

Efficient photon confinement: PIN structure with smaller n for P, N regions



Smaller E_g material has larger n ($n_1 > n_2$)

→ Dielectric waveguide!

=> More photons interacting with injected electrons and holes in the active region

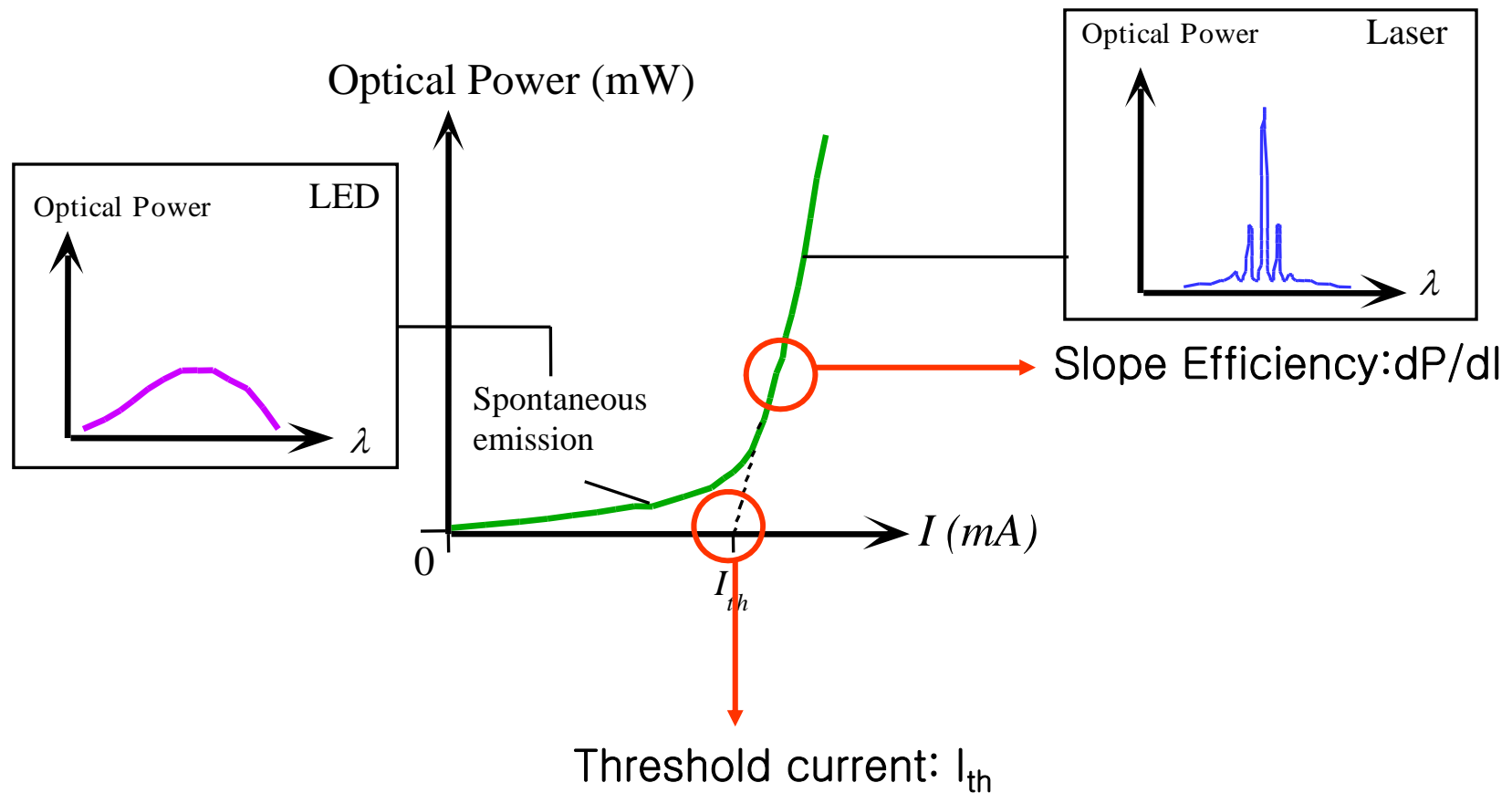
→ larger Γ

With $\Gamma < 1$,

$$g_{th} = \frac{1}{L} \ln \frac{1}{R} = \alpha_m \text{ (mirror loss)} \Rightarrow \Gamma g_{th} = \frac{1}{L} \ln \frac{1}{R} = \alpha_m$$

$$\frac{\lambda}{n} = \frac{2L}{m} \Rightarrow \frac{\lambda}{n_{eff}} = \frac{2L}{m}; \quad n_{eff} = \frac{\beta}{k_0}$$

Lect. 22: Semiconductor Lasers



Lect. 22: Semiconductor Lasers

Analytical expression for I_{th}

Assume optical gain increases linearly with injected carriers: $g = a(N - N_0)$

1) Determine carrier density (N_{th}) required for g_{th} :

$$N_{th} = \frac{g_{th}}{a} + N_0, \quad g_{th} = \frac{\alpha_m}{\Gamma} \quad \therefore N_{th} = \frac{\alpha_m}{\Gamma a} + N_0$$

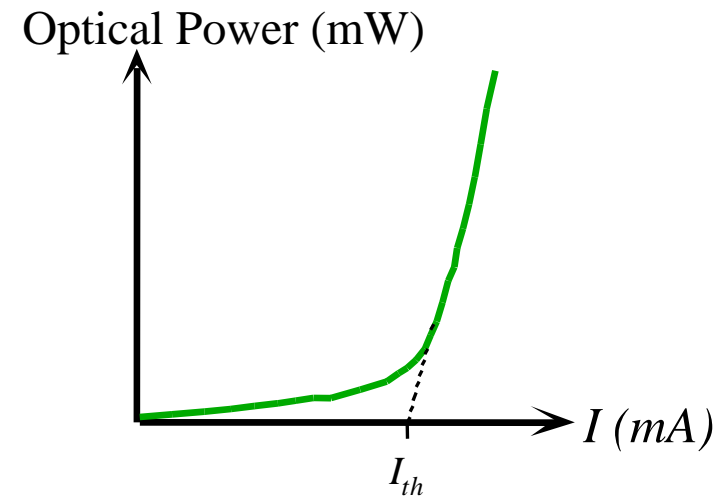
2) Relationship between I and N

$$\frac{dN}{dt} = \frac{I}{qV} - \frac{N}{\tau} \quad \text{In steady-state, } I = \frac{N}{\tau} \cdot qV$$

(V : volume of active region, τ : carrier life time)

3) Determine I_{th} from N_{th} assuming steady-state

$$\therefore I_{th} = \frac{N_{th}}{\tau} \cdot qV = \left(\frac{\alpha_m}{\Gamma a} + N_0 \right) \frac{1}{\tau} \cdot qV$$



Lect. 22: Semiconductor Lasers

Analytical expression for dP/dI

- Assume injected carriers are all converted into photons by stimulated emission when $I > I_{th}$
- Change in photon density with time

$$\frac{dn_{ph}}{dt} = \frac{I - I_{th}}{qV} - \frac{n_{ph}}{\tau_{ph}} \quad \tau_{ph} = \frac{1}{v \cdot \alpha_m}$$

- At steady-state,

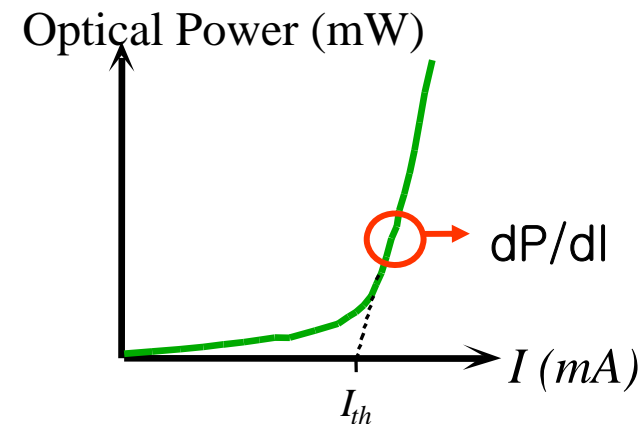
$$n_{ph} = \frac{I - I_{th}}{qV} \cdot \tau_{ph}$$

- How many photons out of laser per second?

$$\Rightarrow \frac{n_{ph}V}{\tau_{ph}}$$

- Output power

$$P_{out} = \frac{\hbar\omega n_{ph}V}{\tau_{ph}} = \hbar\omega \frac{I - I_{th}}{qV} \cdot \tau_{ph} \frac{V}{\tau_{ph}} = \hbar\omega \frac{I - I_{th}}{q} \quad \therefore \frac{dP}{dI} = \frac{\hbar\omega}{q}$$

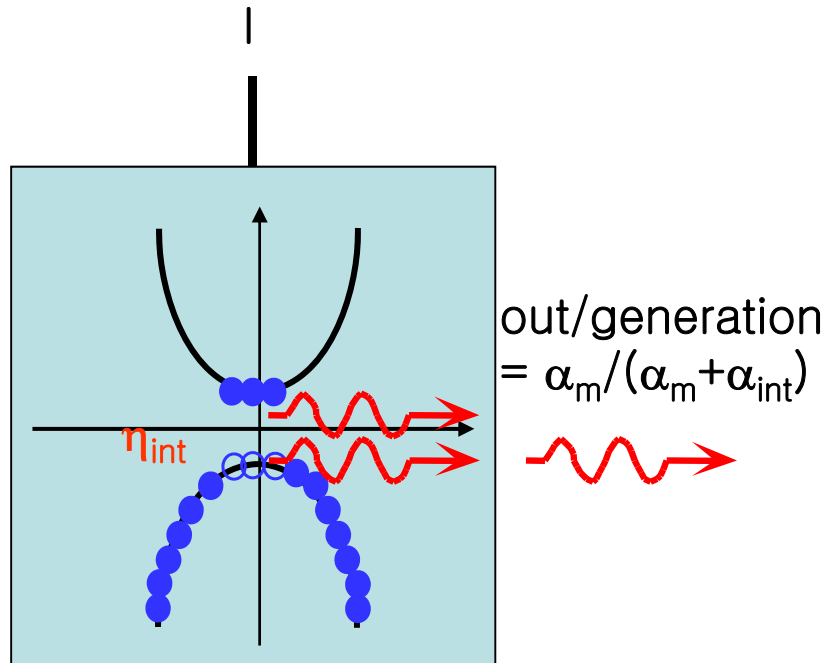


Lect. 22: Semiconductor Lasers

More detailed model:

- Injected carriers are not 100% converted into photons: conversion efficiency, η_{int}
- Photons can be lost internally by impurities, scattering, ... : internal loss, α_{int}

Modifications:



$$g_{\text{th}} : \frac{\alpha_m}{\Gamma} \implies \frac{\alpha_m + \alpha_{\text{int}}}{\Gamma} \quad I_{\text{th}} = \left(\frac{\alpha_m + \alpha_{\text{int}}}{\Gamma a} + N_0 \right) \frac{1}{\tau} \cdot qV$$

$$n_{\text{ph}} : \frac{I - I_{\text{th}}}{qV} \cdot \tau_{\text{ph}} \implies \eta_{\text{int}} \frac{I - I_{\text{th}}}{qV} \cdot \tau_{\text{ph}}$$

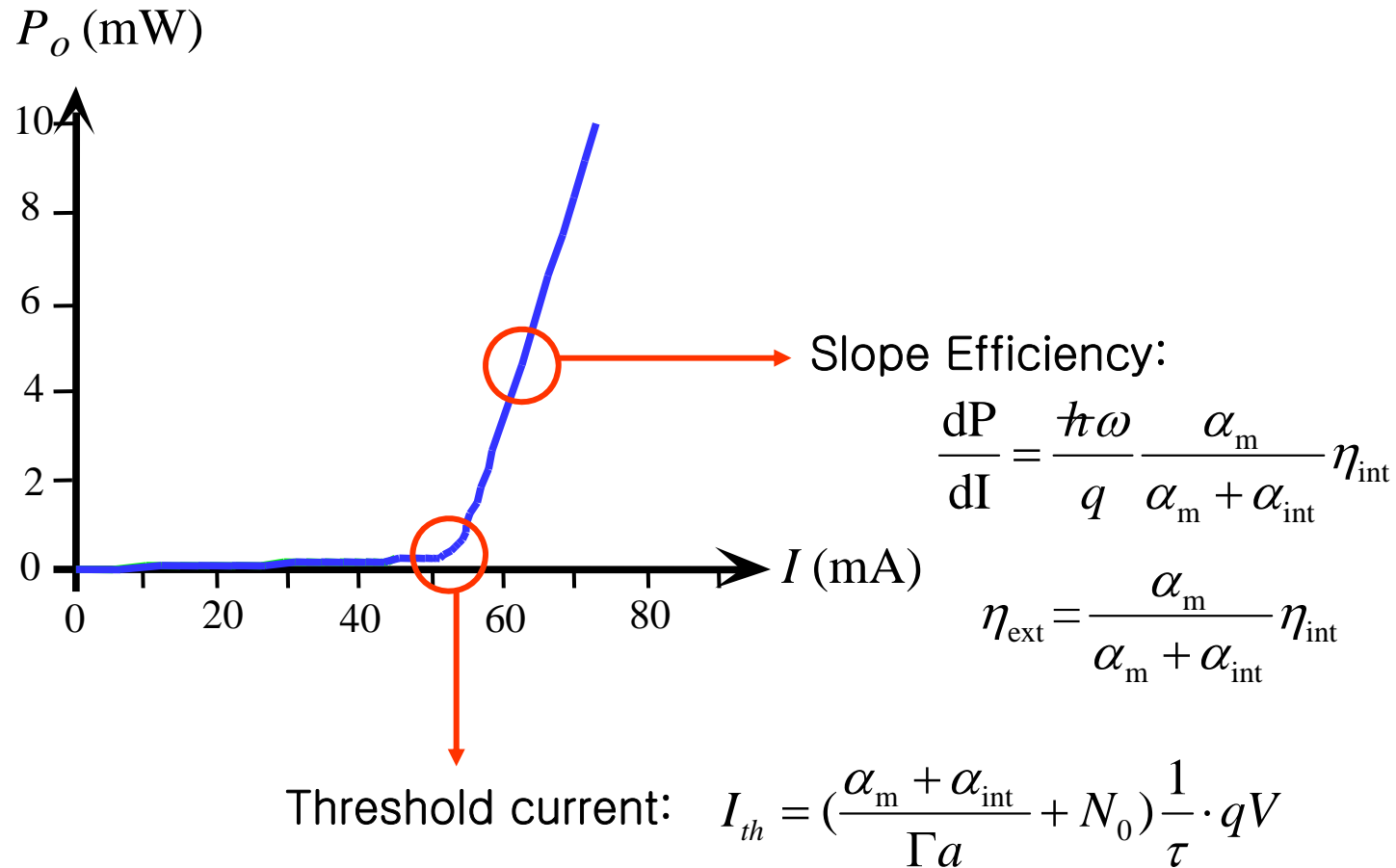
$$\tau_{\text{ph}} = \frac{1}{v \cdot \alpha_m} \implies \frac{1}{v \cdot (\alpha_m + \alpha_{\text{int}})}$$

$$P_{\text{out}} : \frac{\hbar \omega n_{\text{ph}} V}{\tau_{\text{ph}}} \implies \frac{\hbar \omega n_{\text{ph}} V}{\tau_{\text{ph},m}} \quad \text{with } \tau_{\text{ph},m} = \frac{1}{v \cdot \alpha_m}$$

$$P_{\text{out}} = \hbar \omega \cdot \left(\eta_{\text{int}} \frac{I - I_{\text{th}}}{qV} \tau_{\text{ph}} \right) \frac{V}{\tau_{\text{ph},m}} = \frac{\hbar \omega}{q} \cdot \frac{\tau_{\text{ph}}}{\tau_{\text{ph},m}} \cdot \eta_{\text{int}} (I - I_{\text{th}})$$

$$= \frac{\hbar \omega}{q} \frac{\alpha_m}{\alpha_m + \alpha_{\text{int}}} \eta_{\text{int}} (I - I_{\text{th}})$$

Lect. 22: Semiconductor Lasers



Lect. 22: Semiconductor Lasers

Homework:

A semiconductor laser has following properties.

- Cavity length: 500 μm
- Active region thickness: 0.2 μm
- Active region width: 2 μm
- Confinement factor: 0.15
- Internal loss: 6 cm^{-1}
- Mirror reflectivity (both facets): 0.3
- Effective index: 3.5
- Carrier lifetime at threshold: 2 nsec

The gain characteristics for the active region material are shown in the figure shown below.
Answer the following questions. Use interpolation when necessary.

- (a) What is the threshold gain in cm^{-1} for the laser?
- (b) At what wavelength can the first lasing mode be observed?
- (c) Estimate the threshold current for the first lasing mode.
- (d) As the injected current increases, more than one lasing modes are observed. What is the mode separation in nm?

Lect. 22: Semiconductor Lasers

Homework:

