

## Quiz #10 (Wave Packet)

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Quantum Mechanics

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### Prob. 1(2)

What is the relationship between angular frequency ( $\omega$ ) and wave number ( $k$ ) for each of following waves? Determine its phase velocity and group velocity.

(a) A particle with mass  $M$  in free space.

(b) An electro-magnetic wave in a vacuum.

### Prob. 2(1)

The phase velocity of light in some material around  $\omega_0$  is given as

$v_p(\omega) = v_0 \frac{\omega_0}{\omega_0 + a(\omega - \omega_0)}$ , where  $v_0$  and  $a$  are constants. What is the group

velocity of light in this material,  $v_g(\omega)$ , at  $\omega = \omega_0$ ?

### Prob.3(2)

Determine whether each of following statements is true or not. Explain.

(a) A Gaussian wave packet representing a particle located in a free space gets broadened as time increases.

(b) The magnitude of the group velocity for a particle with mass  $M$  in the ground state of an infinite barrier quantum well having width  $L$  is  $h/(2mL)$ , where  $h$  is the Planck's constant.