

# **Opto-Electronics and Photonics**

## **Lecture 5: Polarization**

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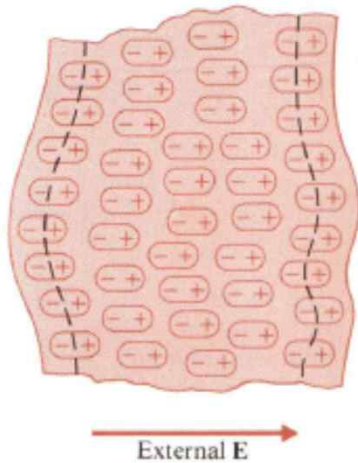
**Dept. of Electrical and Electronic Engineering  
Yonsei University**

# Lecture 5: Polarization

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## Polarization (Lecture 2)

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## Polarization:

How E-, H-field directions change with time

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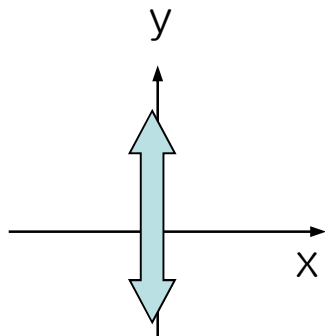
# Lecture 5: Polarization

Consider  $\bar{E} = (\bar{x}E_1 + \bar{y}E_2) e^{jkz} e^{j\omega t}$

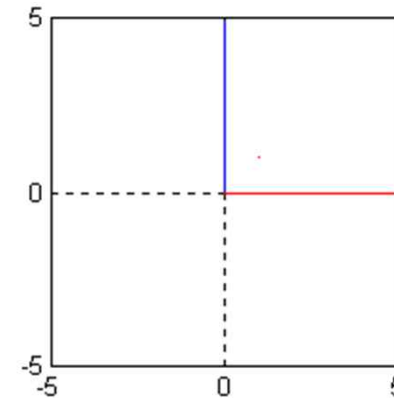
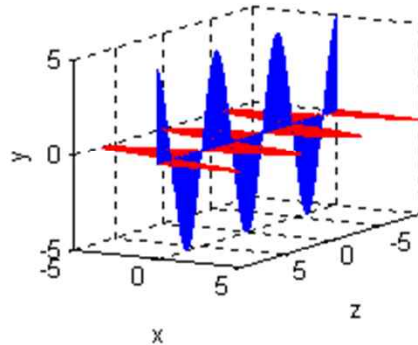
How does E-field direction change in time?

Let  $z=0$   $\text{Re}[\bar{E}] = \bar{x}E_1 \cos(\omega t) + \bar{y}E_2 \cos(\omega t)$

1) If  $E_1=0$  :  $\text{Re}[\bar{E}] = \bar{y}E_2 \cos(\omega t)$



Linear polarization

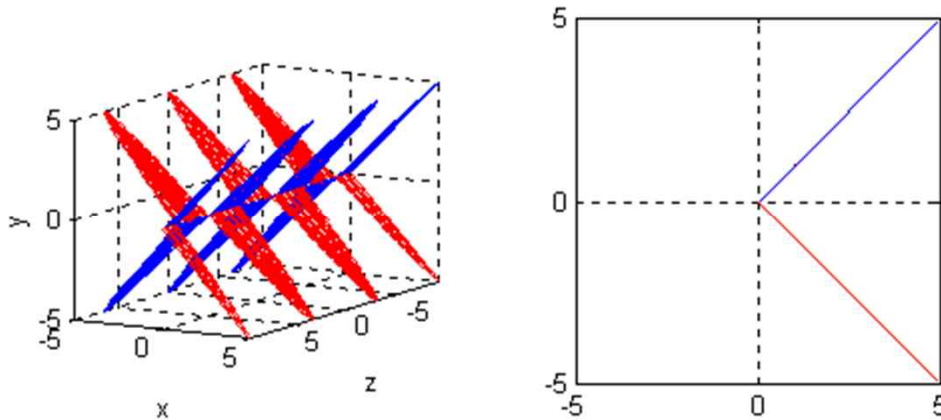


# Lecture 5: Polarization

$$\bar{E} = (\bar{x}E_1 + \bar{y}E_2) e^{jkz} e^{j\omega t}$$

$$2) E_1 = E_2 \quad \bar{E} = (\bar{x} + \bar{y}) E_1 e^{jkz} e^{j\omega t}$$

$$\text{At } z=0, \text{ Re}[\bar{E}] = \bar{x}E_1 \cos(\omega t) + \bar{y}E_1 \cos(\omega t)$$



Linear Polarization

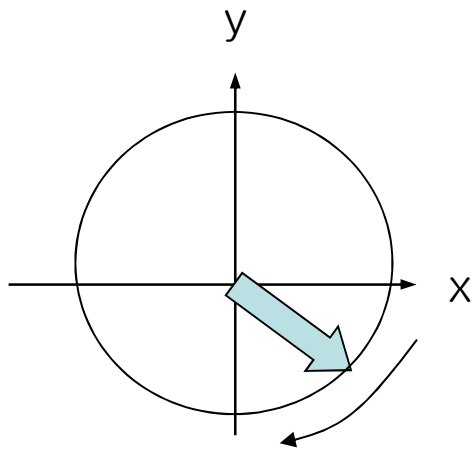
# Lecture 5: Polarization

$$\bar{E} = (\bar{x}E_1 + \bar{y}E_2) e^{jkz} e^{j\omega t}$$

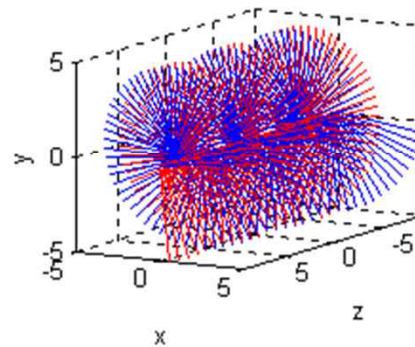
$$3) E_2 = j E_1 \quad \bar{E} = (\bar{x} + \bar{y}j) E_1 e^{jkz} e^{j\omega t}$$

At  $z=0$ ,

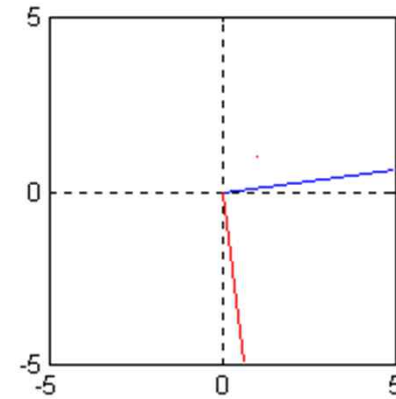
$$\begin{aligned} \text{Re}(\bar{E}) &= \text{Re} \left[ E_1 \left( \bar{x}e^{j\omega t} + \bar{y}e^{j(\omega t + \pi/2)} \right) \right] = E_1 \left\{ \bar{x} \cos(\omega t) + \bar{y} \cos(\omega t + \pi / 2) \right\} \\ &= E_1 \left\{ \bar{x} \cos(\omega t) - \bar{y} \sin(\omega t) \right\} \end{aligned}$$



Circular polarization



Right-Handed Circular Polarization (RHCP)

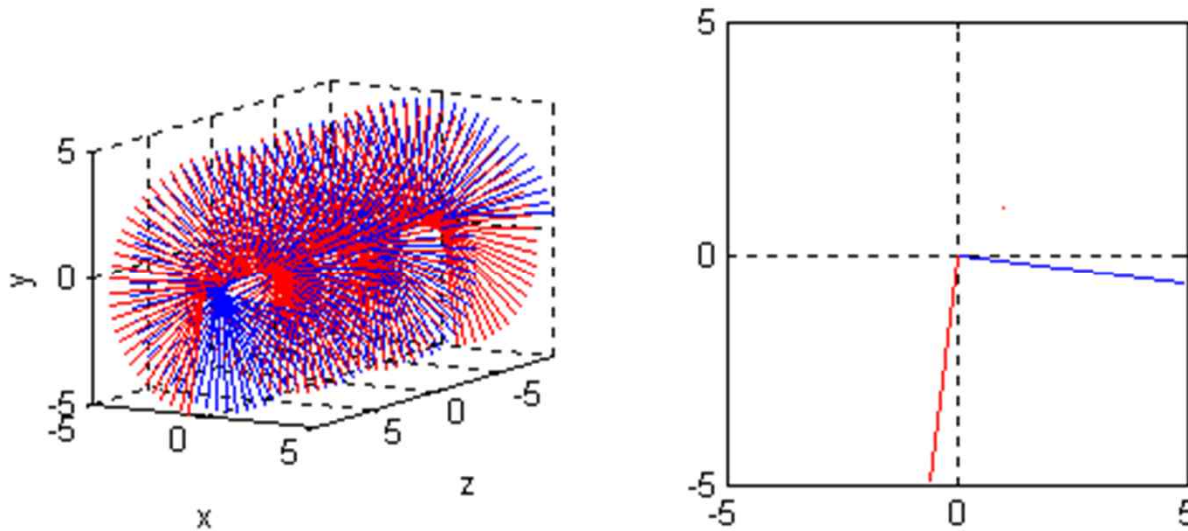


# Lecture 5: Polarization

$$\bar{E} = (\bar{x} + \bar{y}j) E_1 e^{jkz} e^{j\omega t} \implies E_1 \{ \bar{x} \cos(\omega t) - \bar{y} \sin(\omega t) \} \quad \text{RHCH}$$

$$\bar{E} = (\bar{x} - \bar{y}j) E_1 e^{jkz} e^{j\omega t}$$

$$\text{At } z=0, \quad \text{Re}(\bar{E}) = E_1 \{ \bar{x} \cos(\omega t) + \bar{y} \sin(\omega t) \}$$

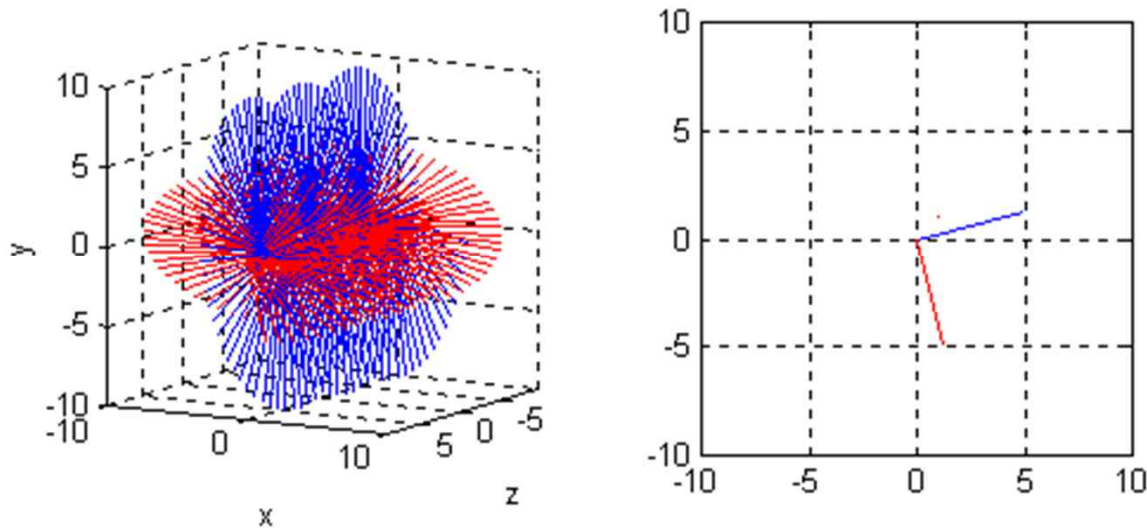


Left-Handed Circular Polarization (LHCP)

# Lecture 5: Polarization

4) If  $E_1 < E_2$

$$\bar{E} = (\bar{x}E_1 + \bar{y}jE_2)e^{jkz}e^{j\omega t}$$

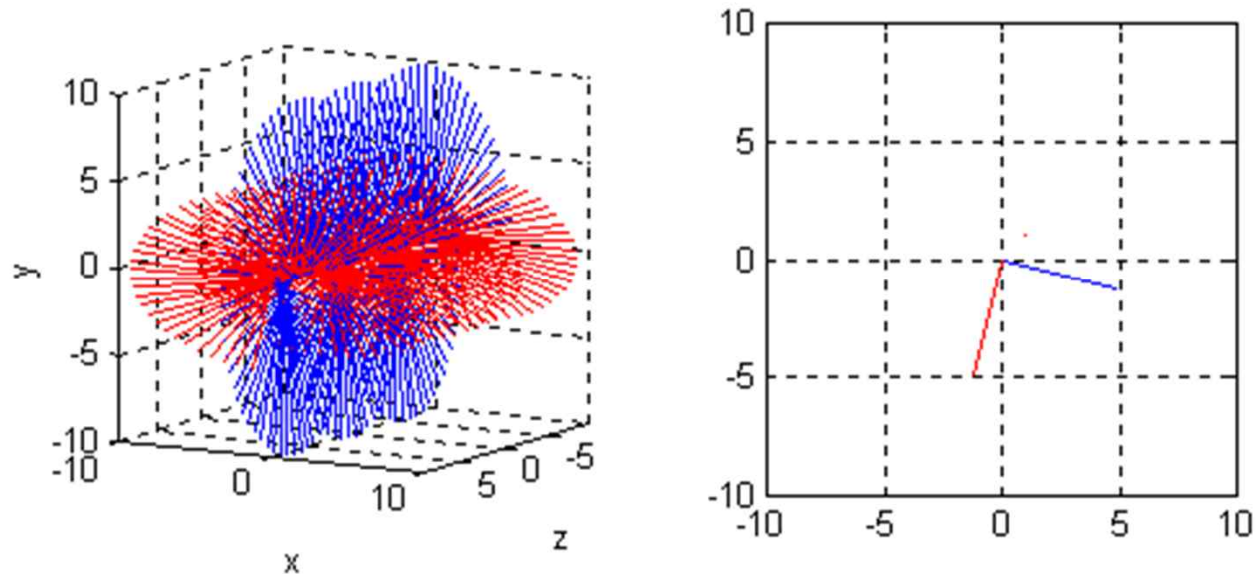


Right-Handed Elliptical Polarization

# Lecture 5: Polarization

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$$\vec{E} = (\bar{x}E_1 - \bar{y}jE_2)e^{jkz}e^{j\omega t}$$



Left-Handed Elliptical Polarization

# Lecture 5: Polarization

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$$\bar{E} = (\bar{x}E_1 + \bar{y}E_2) e^{jkz} e^{j\omega t}$$

$$E_1 = |E_1| \exp(j\theta_1), \quad E_2 = |E_2| \exp(j\theta_2)$$

If  $\theta_1 = \theta_2$ , linear

else if ( $|E_1| = |E_2|$  and  $|\theta_2 - \theta_1| = \pi/2$ ), circular

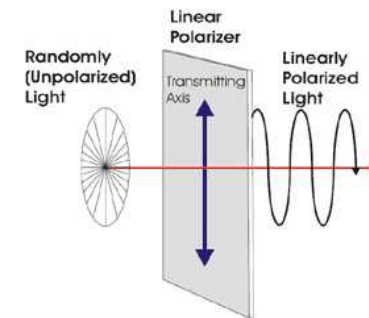
otherwise elliptical

# Lecture 5: Polarization

Polarization is an important property of EM waves

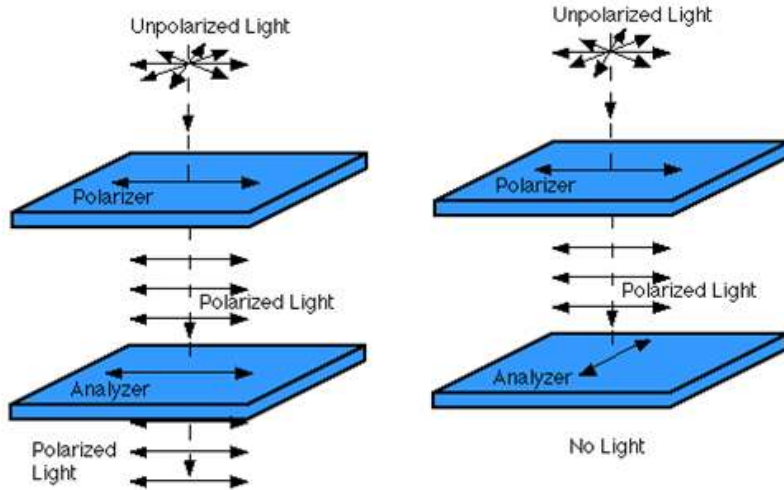


Polarization Filters

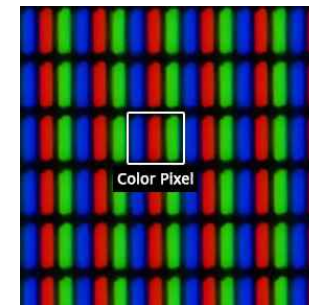
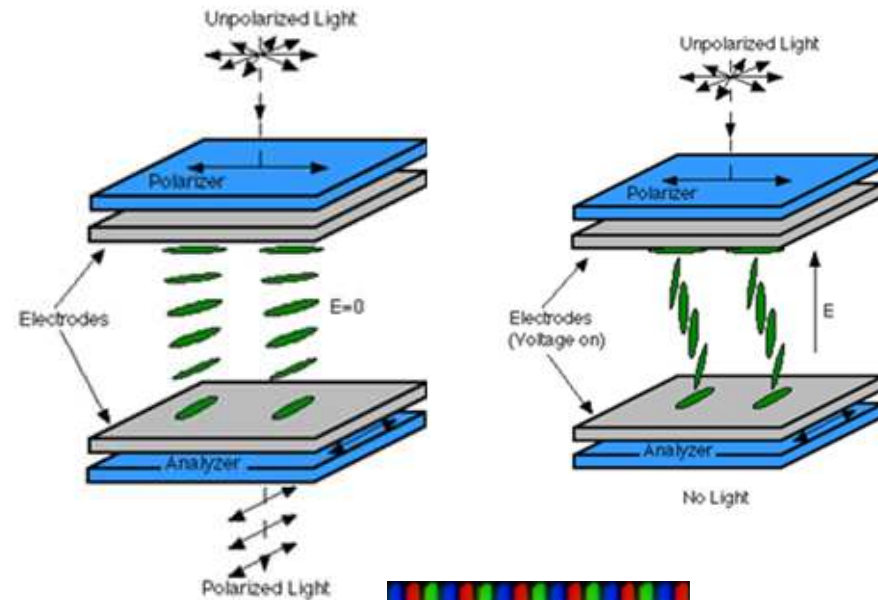


# Lecture 5: Polarization

Turning on/off light transmission



Liquid Crystal Display



# Lecture 5: Polarization

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Homework (Due 9/20)

(1) What is the polarization of  $\bar{E} = (\bar{x} + \bar{y})E_0e^{-jkz}e^{j\omega t}$  ?

(2) What is the polarization of  $\bar{E} = (\bar{x}j + \bar{y})E_0e^{-jkz}e^{j\omega t}$  ?

(3) What is the polarization of  $\bar{E} = \left(\bar{x}j + \frac{\bar{y} - \bar{z}}{\sqrt{2}}\right)E_0e^{-j\frac{k}{\sqrt{2}}y}e^{-j\frac{k}{\sqrt{2}}z}e^{j\omega t}$  ?

(4) Show that a linearly polarized plane wave can be expressed as a sum of RHC and LHC waves